



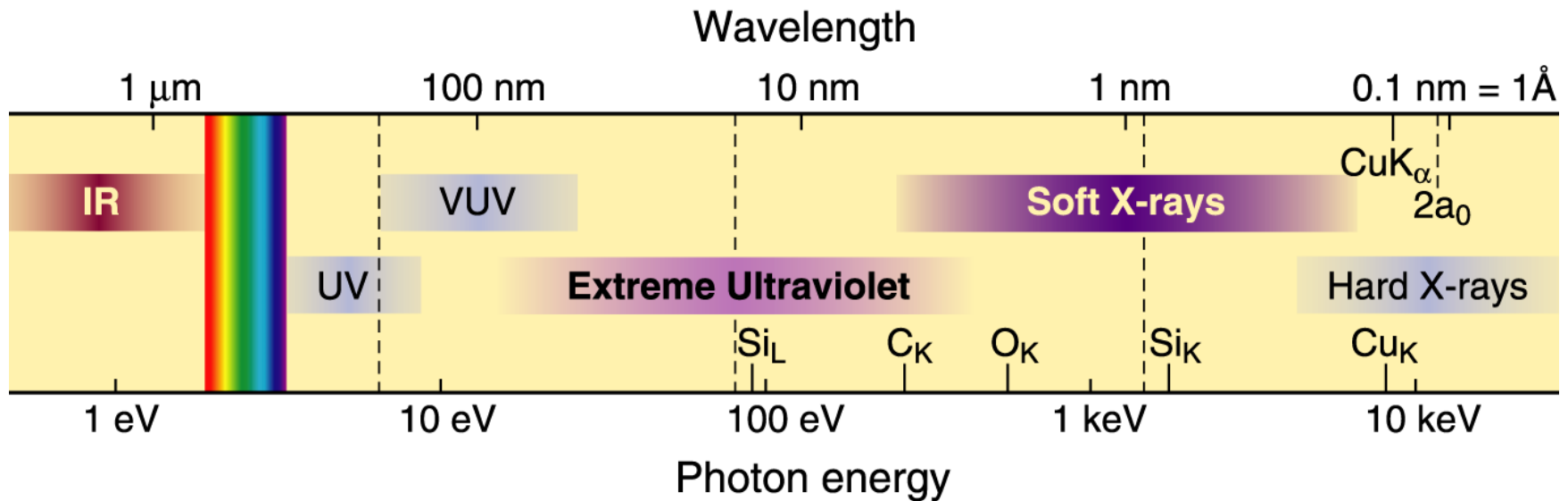
Introduction to Synchrotron Radiation and Beamlines

David Attwood
University of California, Berkeley

<http://ast.coe.berkeley.edu/sxr2009>

<http://ast.coe.berkeley.edu/srms>

The short wavelength region of the electromagnetic spectrum

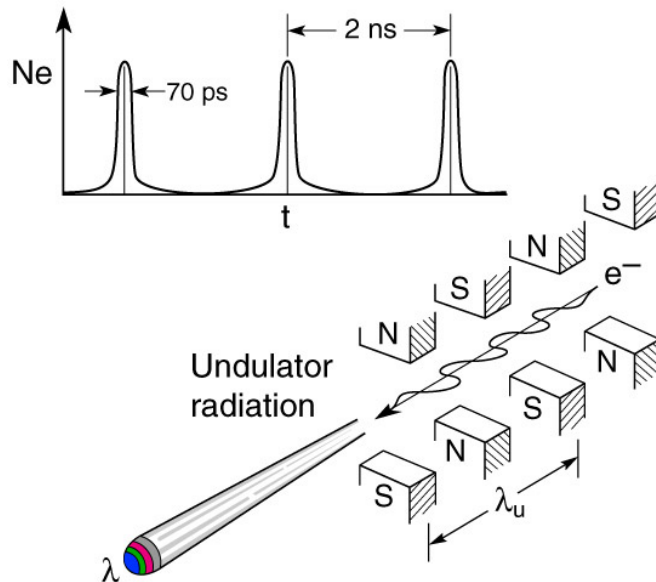
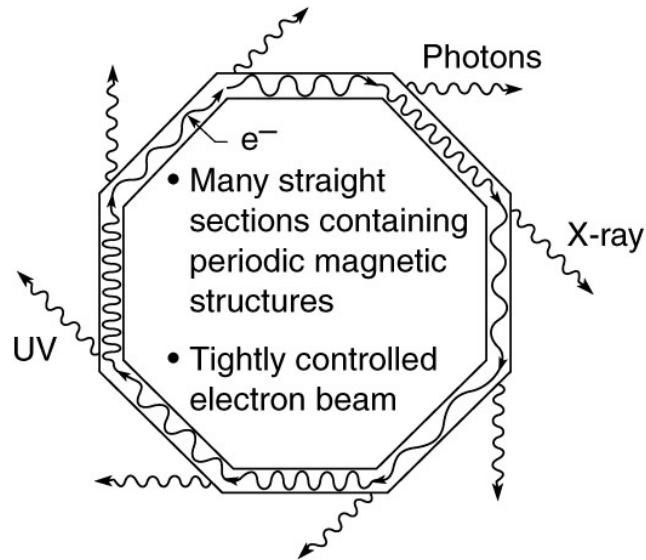


- See smaller features
- Write smaller patterns
- Elemental and chemical sensitivity

$$\hbar\omega \cdot \lambda = hc = 1239.842 \text{ eV nm}$$

$$n = 1 - \delta + i\beta \quad \delta, \beta \ll 1$$

Synchrotron radiation



Bending Magnet:

$$\hbar\omega_c = \frac{3e\hbar B\gamma^2}{2m} \quad (5.7)$$

Wiggler:

$$\hbar\omega_c = \frac{3e\hbar B\gamma^2}{2m} \quad (5.80)$$

$$n_c = \frac{3K}{4} \left(1 + \frac{K^2}{2}\right) \quad (5.82)$$

$$P_T = \frac{\pi e K^2 \gamma^2 I N}{3\epsilon_0 \lambda_u} \quad (5.85)$$

Undulator:

$$\lambda = \frac{\lambda_u}{2\gamma^2} \left(1 + \frac{K^2}{2} + \gamma^2\theta^2\right) \quad (5.28)$$

$$K = \frac{eB_0\lambda_u}{2\pi mc} \quad (5.18)$$

$$\theta_{cen} = \frac{1}{\gamma^*\sqrt{N}} \quad (5.15)$$

$$\left.\frac{\Delta\lambda}{\lambda}\right|_{cen} = \frac{1}{N} \quad (5.14)$$

$$\bar{P}_{cen} = \frac{\pi e \gamma^2 I}{\epsilon_0 \lambda_u} \frac{K^2}{\left(1 + \frac{K^2}{2}\right)^2} f(K) \quad (5.41)$$

Ch05_F00VG_Jan06.ai

Electron binding energies, in electron volts (eV), for the elements in their natural forms

Element	K 1s	L ₁ 2s	L ₂ 2p _{1/2}	L ₃ 2p _{3/2}	M ₁ 3s	M ₂ 3p _{1/2}	M ₃ 3p _{3/2}	M ₄ 3d _{3/2}	M ₅ 3d _{5/2}	N ₁ 4s	N ₂ 4p _{1/2}	N ₃ 4p _{3/2}
1 H	13.6											
2 He	24.6 ^b											
3 Li	54.7 ^b											
4 Be	111.5 ^b											
5 B	188 ^b											
6 C	284.2 ^b											
7 N	409.9 ^b	37.3 ^b										
8 O	543.1 ^b	41.6 ^b										
9 F	696.7 ^b											
10 Ne	870.2 ^b	48.5 ^b	21.7 ^b	21.6 ^b								
11 Na	1070.8 ^c	63.5 ^c	30.4 ^c	30.5 ^b								
12 Mg	1303.0 ^c	88.6 ^b	49.6 ^c	49.2 ^c								
13 Al	1559.6	117.8 ^b	72.9 ^b	72.5 ^b								
14 Si	1838.9	149.7 ^b	99.8 ^b	99.2 ^b								
15 P	2145.5	189 ^b	136 ^b	135 ^b								
16 S	2472	230.9 ^b	163.6 ^b	162.5 ^b								
17 Cl	2822.4	270.2 ^b	202 ^b	200 ^b								
18 Ar	3205.9 ^b	326.3 ^b	250.6 ^b	248.4 ^b	29.3 ^b	15.9 ^b	15.7 ^b					
19 K	3608.4 ^b	378.6 ^b	297.3 ^b	294.6 ^b	34.8 ^b	18.3 ^b	18.3 ^b					
20 Ca	4038.5 ^b	438.4 ^c	349.7 ^c	346.2 ^c	44.3 ^c	25.4 ^c	25.4 ^c					
21 Sc	4492.8	498.0 ^b	403.6 ^b	398.7 ^b	51.1 ^b	28.3 ^b	28.3 ^b					
22 Ti	4966.4	560.9 ^c	461.2 ^c	453.8 ^c	58.7 ^c	32.6 ^c	32.6 ^c					
23 V	5465.1	626.7 ^c	519.8 ^c	512.1 ^c	66.3 ^c	37.2 ^c	37.2 ^c					
24 Cr	5989.2	695.7 ^c	583.8 ^c	574.1 ^c	74.1 ^c	42.2 ^c	42.2 ^c					
25 Mn	6539.0	769.1 ^c	649.9 ^c	638.7 ^c	82.3 ^c	47.2 ^c	47.2 ^c					
26 Fe	7112.0	844.6 ^c	719.9 ^c	706.8 ^c	91.3 ^c	52.7 ^c	52.7 ^c					
27 Co	7708.9	925.1 ^c	793.3 ^c	778.1 ^c	101.0 ^c	58.9 ^c	58.9 ^c					
28 Ni	8332.8	1008.6 ^c	870.0 ^c	852.7 ^c	110.8 ^c	68.0 ^c	66.2 ^c					
29 Cu	8978.9	1096.7 ^c	952.3 ^c	932.5 ^c	122.5 ^c	77.3 ^c	75.1 ^c					
30 Zn	9658.6	1196.2 ^b	1044.9 ^b	1021.8 ^b	139.8 ^b	91.4 ^b	88.6 ^b	10.2 ^b	10.1 ^b			
31 Ga	10367.1	1299.0 ^b	1143.2 ^c	1116.4 ^c	159.5 ^c	103.5 ^c	103.5 ^c	18.7 ^c	18.7 ^c			
32 Ge	11103.1	1414.6 ^b	1248.1 ^b	1217.0 ^b	180.1 ^b	124.9 ^b	120.8 ^b	29.0 ^b	29.0 ^b			
33 As	11866.7	1527.0 ^b	1359.1 ^b	1323.6 ^b	204.7 ^b	146.2 ^b	141.2 ^b	41.7 ^b	41.7 ^b			
34 Se	12657.8	1652.0 ^b	1474.3 ^b	1433.9 ^b	229.6 ^b	166.5 ^b	160.7 ^b	55.5 ^b	54.6 ^b			
35 Br	13473.7	1782.0 ^b	1596.0 ^b	1549.9 ^b	257 ^b	189 ^b	182 ^b	70 ^b	69 ^b			
36 Kr	14325.6	1921.0	1730.9 ^b	1678.4 ^b	292.8 ^b	222.2 ^b	214.4	95.0 ^b	93.8 ^b	27.5 ^b	14.1 ^b	14.1 ^b
37 Rb	15199.7	2065.1	1863.9	1804.4	326.7 ^b	248.7 ^b	239.1 ^b	113.0 ^b	112 ^b	30.5 ^b	16.3 ^b	15.3 ^b
38 Sr	16104.6	2216.3	2006.8	1939.6	358.7 ^c	280.3 ^c	270.0 ^c	136.0 ^c	134.2 ^c	38.9 ^c	20.3 ^c	20.3 ^c
39 Y	17038.4	2372.5	2155.5	2080.0	392.0 ^b	310.6 ^b	298.8 ^b	157.7 ^c	155.8 ^c	43.8 ^b	24.4 ^b	23.1 ^b
40 Zr	17997.6	2531.6	2306.7	2222.3	430.3 ^c	343.5 ^c	329.8 ^c	181.1 ^c	178.8 ^c	50.6 ^c	28.5 ^c	27.7 ^c
41 Nb	18985.6	2697.7	2464.7	2370.5	466.6 ^c	376.1 ^c	360.6 ^c	205.0 ^c	202.3 ^c	56.4 ^c	32.6 ^c	30.8 ^c
42 Mo	19999.5	2865.5	2625.1	2520.2	506.3 ^c	411.6 ^c	394.0 ^c	231.1 ^c	227.9 ^c	63.2 ^c	37.6 ^c	35.5 ^c
43 Tc	21044.0	3042.5	2793.2	2676.9	544 ^b	445 ^b	425 ^b	257 ^b	253 ^b	68 ^b	39 ^c	39 ^b
44 Ru	22117.2	3224.0	2966.9	2837.9	586.2 ^c	483.5 ^c	461.4 ^c	284.2 ^c	280.0 ^c	75.0 ^c	46.5 ^c	43.2 ^c
45 Rh	23219.9	3411.9	3146.1	3003.8	628.1 ^c	521.3 ^c	496.5 ^c	311.9 ^c	307.2 ^c	81.4 ^b	50.5 ^c	47.3 ^c
46 Pd	24350.3	3604.3	3330.3	3173.3	671.6 ^c	559.9 ^c	532.3 ^c	340.5 ^c	335.2 ^c	87.6 ^b	55.7 ^c	50.9 ^c
47 Ag	25514.0	3805.8	3523.7	3351.1	719.0 ^c	603.8 ^c	573.0 ^c	374.0 ^c	368.0 ^c	97.0 ^c	63.7 ^c	58.3 ^c

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Broadly tunable radiation is needed to probe the primary (n = 1 & n = 2) resonances of the elements



Group
IA

1

1.0079

1

H

1s¹

Hydrogen

IIA

3

6.941

1

Li

1s² 2s¹

Lithium

4

9.012

1

Be

1s² 2s²

Beryllium

11

22.990

1

Na

[Ne]3s¹

Sodium

12

24.31

2

Mg

[Ne]3s²

Magnesium

19

39.098

1

K

[Ar]4s¹

Potassium

20

40.08

2

Ca

[Ar]4s²

Calcium

21

44.96

3

Sc

[Ar]3d¹4s²

Scandium

22

47.88

4

Ti

[Ar]3d²4s²

Titanium

23

50.94

5, 4, 3, 2

V

[Ar]3d³4s²

Vanadium

24

52.00

6, 3, 2

Cr

[Ar]3d⁵4s¹

Chromium

25

54.94

7, 6, 4, 2, 3

Mn

[Ar]3d⁵4s²

Manganese

26

55.85

2, 3

Fe

[Ar]3d⁶4s²

Iron

27

58.93

2, 3

Co

[Ar]3d⁷4s²

Cobalt

28

58.69

2, 3

Ni

[Ar]3d⁸4s²

Nickel

29

63.55

2, 1

Cu

[Ar]3d¹⁰4s¹

Copper

30

65.39

2

Zn

[Ar]3d¹⁰4s²

Zinc

31

69.72

3

Ga

[Ar]3d¹⁰4s²4p¹

Gallium

32

72.61

4

Ge

[Ar]3d¹⁰4s²4p²

Germanium

33

74.92

3, 5

As

[Ar]3d¹⁰4s²4p³

Arsenic

34

78.96

~2, 4, 6

Se

[Ar]3d¹⁰4s²4p⁴

Selenium

35

79.904

1, 5

Br

[Ar]3d¹⁰4s²4p⁵

Bromine

36

83.80

1

Kr

[Ar]3d¹⁰4s²4p⁶

Krypton

37

85.47

1

Rb

[Kr]5s¹

Rubidium

38

87.62

2

Sr

[Kr]5s²

Strontium

39

88.91

3

Y

[Kr]4d¹5s²

Yttrium

40

91.22

4

Zr

[Kr]4d²5s²

Zirconium

41

92.91

5

Nb

[Kr]4d⁴5s¹

Niobium

42

95.94

6, 3, 2

Mo

[Kr]4d⁵5s¹

Molybdenum

43

(98)

7

Tc

[Kr]4d⁵5s¹

Technetium

44

101.1

2, 3, 4, 6, 8

Ru

[Kr]4d⁶5s¹

Ruthenium

45

102.91

2, 3, 4

Rh

[Kr]4d⁷5s¹

Rhodium

46

106.4

2, 4

Pd

[Kr]4d¹⁰

Palladium

47

107.87

1

Ag

[Kr]4d¹⁰5s¹

Silver

48

112.41

2

Cd

[Kr]4d¹⁰5s²

Cadmium

49

114.82

3

In

[Kr]4d¹⁰5s²5p¹

Indium

50

118.71

4, 2

Sn

[Kr]4d¹⁰5s²5p²

Tin

51

121.76

3, 5

Sb

[Kr]4d¹⁰5s²5p³

Antimony

52

127.60

~2, 4, 6

Te

[Kr]4d¹⁰5s²5p⁴

Tellurium

53

126.90

1, 5, 7

I

[Kr]4d¹⁰5s²5p⁵

Iodine

54

131.29

1

Xe

[Kr]4d¹⁰5s²5p⁶

Xenon

55

132.91

1

Cs

[Xe]6s¹

Cesium

56

137.33

2

Ba

[Xe]6s²

Barium

57

138.91

3

La

[Xe]5d¹6s²

Lanthanum

58

140.12

3, 4

Ce

[Xe]4f¹5d¹6s²

Cerium

59

140.91

3, 4

Pr

[Xe]4f³6s²

Praseodymium

60

144.24

3

Nd

[Xe]4f⁴6s²

Neodymium

61

(145)

3

Pm

[Xe]4f⁵6s²

Promethium

62

150.36

3, 2

Sm

[Xe]4f⁶6s²

Samarium

63

152.0

3, 2

Eu

[Xe]4f⁷6s²

Europium

64

157.25

3

Gd

[Xe]4f⁷5d¹6s²

Gadolinium

65

158.93

3, 4

Tb

[Xe]4f⁹6s²

Terbium

66

162.50

3

Dy

[Xe]4f¹⁰6s²

Dysprosium

67

164.93

3

Ho

[Xe]4f¹¹6s²

Holmium

68

167.26

3

Er

[Xe]4f¹²6s²

Erbium

69

168.93

3, 2

Tm

[Xe]4f¹³6s²

Thulium

70

173.04

2

Yb

[Xe]4f¹⁴6s²

Ytterbium

71

174.97

3

Lu

[Xe]4f¹⁴5d¹6s²

Lutetium

90

232.05

4

Th

[Rn]6d²7s²

Thorium

91

231.04

5, 4

Pa

[Rn]5f²6d¹7s²

Protactinium

92

238.03

6, 5, 4, 3

U

[Rn]5f³6d¹7s²

Uranium

93

(237)

6, 5, 4, 3

Np

[Rn]5f⁴6d¹7s²

Neptunium

94

(244)

6, 5, 4, 3

Pu

[Rn]5f⁶7s²

Plutonium

95

(243)

6, 5, 4, 3

Am

[Rn]5f⁷7s²

Americium

96

(247)

3

Cm

[Rn]5f⁶7s²

Curium

97

(247)

4, 3

Bk

[Rn]5f⁷7s²

Berkelium

98

(251)

3

Cf

[Rn]5f⁸7s²

Californium

99

(252)

3

Es

[Rn]5f⁹7s²

Einsteinium

100

(257)

3

Fm

[Rn]5f¹⁰7s²

Fermium

101

(258)

3

Md

[Rn]5f¹¹7s²

Mendelevium

102

(259)

3

No

[Rn]5f¹²7s²

Nobelium

103

(262)

3

Lr

[Rn]5f¹³7s²

Lawrencium

Key

Atomic number

Atomic weight

Oxidation states
(Bold most stable)

Symbol

Electron configuration

Density (g/cm³)

Concentration (10²²atoms/cm³)

Nearest neighbor (Å)

Name

14

28.09

4

Si

[Ne]3s²3p²

Silicon

█ Solid

█ Gas

█ Liquid

█ Synthetically prepared

References: International Tables for X-ray Crystallography (Reidel, London, 1983) (Ref. 44) and J.R. De Laeter and K.G. Heumann (Ref. 46, 1991).

VIII

2

4.003

1

He

1s²

Helium

IIIB

5

10.81

3

B

1s² 2s² 2p¹

Boron

IVB

6

12.011

4, 2

C

1s² 2s² 2p²

Carbon

VB

7

14.007

3, 5, 4, 2

N

1s² 2s² 2p³

Nitrogen

VIB

8

16

~2

O

1s² 2s² 2p⁴

Oxygen

VIIB

9

19.00

~1

F

1s² 2s² 2p⁵

Fluorine

10

20.180

1

Ne

1s² 2s² 2p⁶

Neon

13

26.98

3

Al

[Ne]3s²3p¹

Aluminum

14

28.09

4

Si

[Ne]3s²3p²

Silicon

15

30.974

3, 5, 4

P

[Ne]3s²3p³

Phosphorus

16

32.066

2, 4, 6

S

[Ne]3s²3p⁴

Sulfur

17

35.453

1, 3, 5, 7

Cl

[Ne]3s²3p⁵

Chlorine

18

39.948

1, 3, 5, 7

Ar

[Ne]3s²3p⁶

Argon

Typical applications of synchrotron radiation

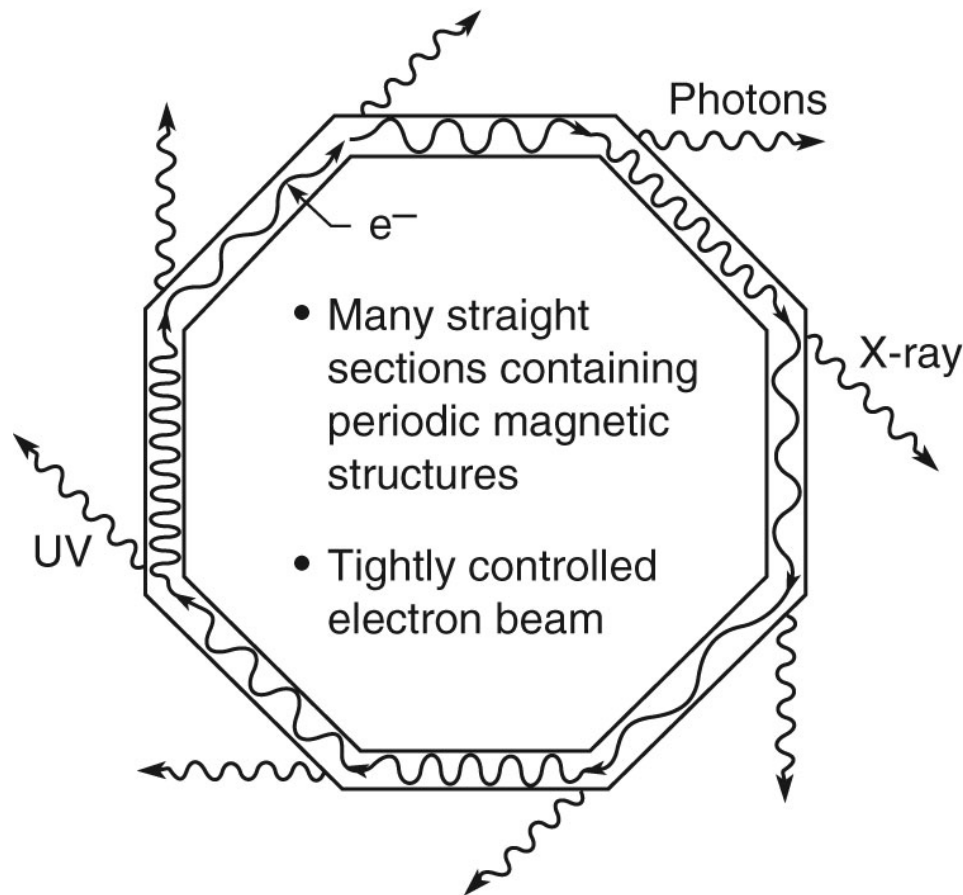


- Surface science
- Magnetic materials
- Materials chemistry
- Environmental sciences
- Protein crystallography
- Biomicroscopy
- Chemical dynamics

3rd Generation facilities, like Elettra, have many straight sections and a small electron beam



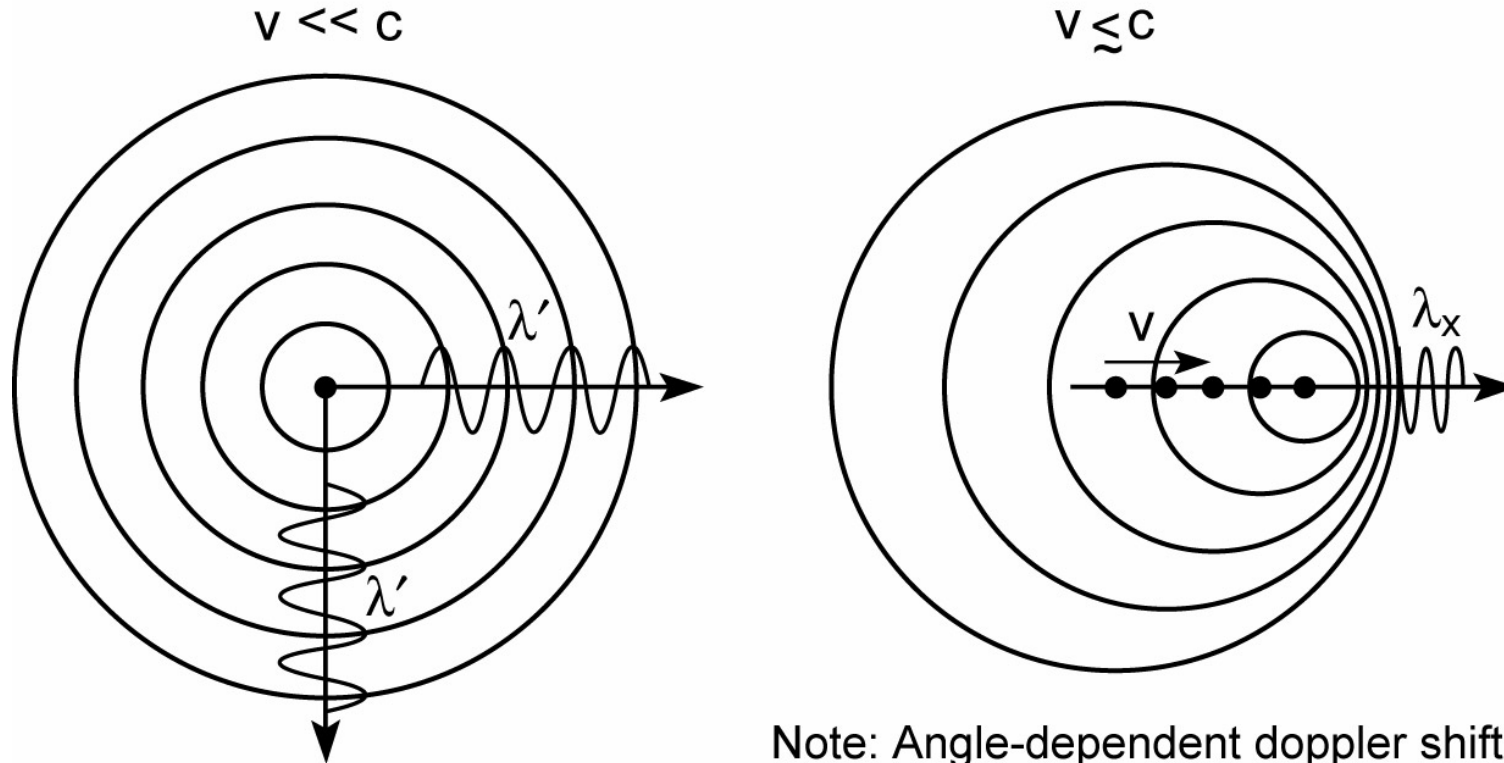
Modern Synchrotron Radiation Facility



- Many straight sections for undulators and wigglers
- Brighter radiation for spatially resolved studies (smaller beam more suitable for microscopies)
- Interesting coherence properties at very short wavelengths

3rdGenFacilitiesrev3.04.ai

Synchrotron radiation from relativistic electrons



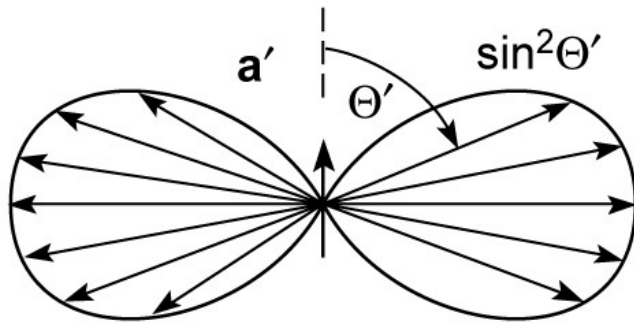
Note: Angle-dependent doppler shift

$$\lambda = \lambda' \left(1 - \frac{v}{c} \cos\theta\right) \quad \lambda = \lambda' \gamma \left(1 - \frac{v}{c} \cos\theta\right)$$

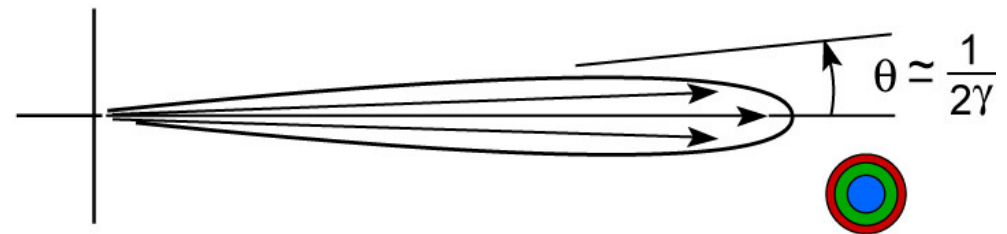
$$\gamma = \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}}$$

Synchrotron radiation in a narrow forward cone

Frame moving with electron



Laboratory frame of reference

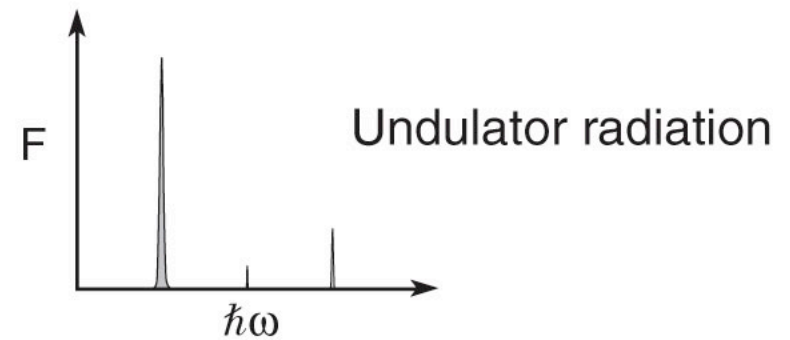
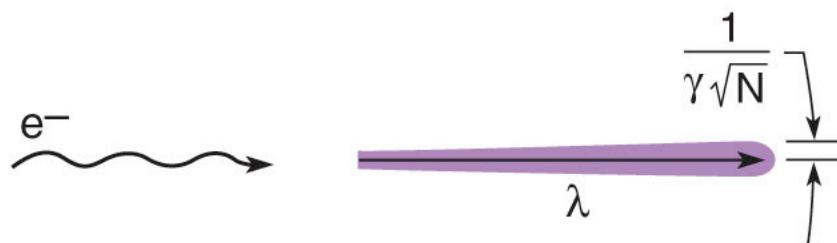
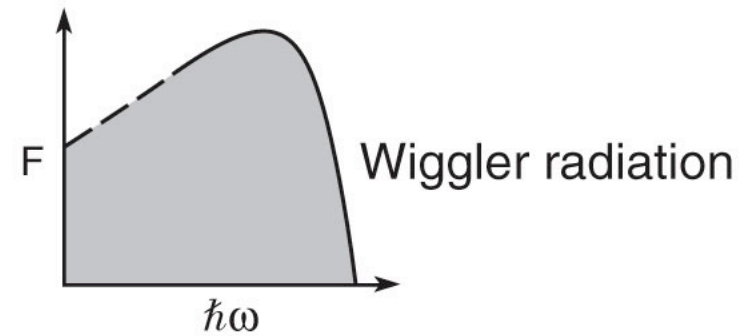
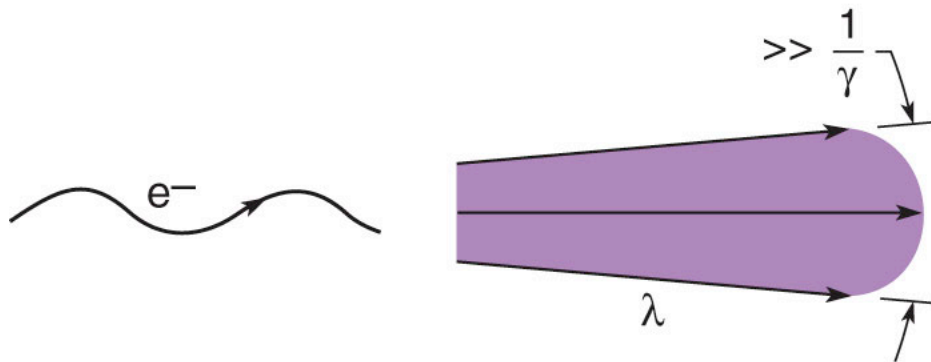
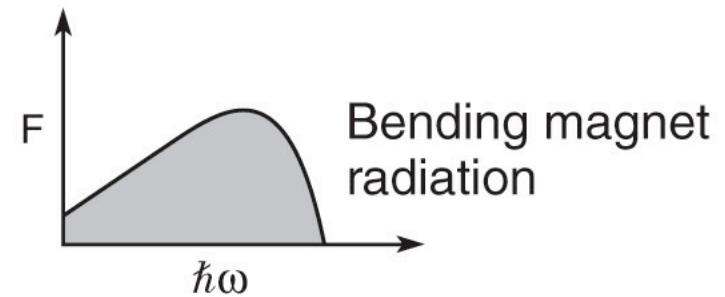
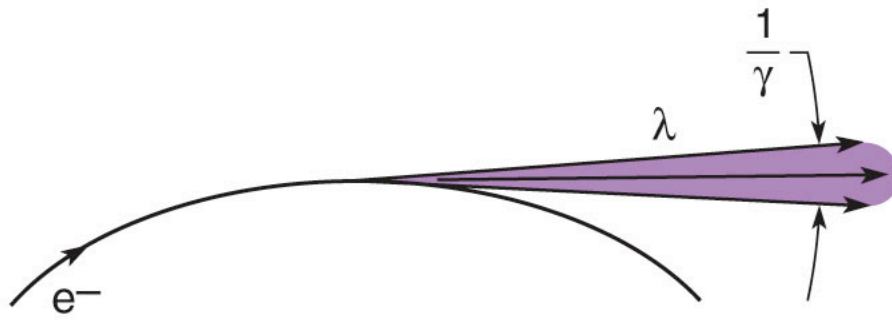


$$\tan \theta = \frac{\sin \theta'}{\gamma(\beta + \cos \theta')} \quad (5.1)$$

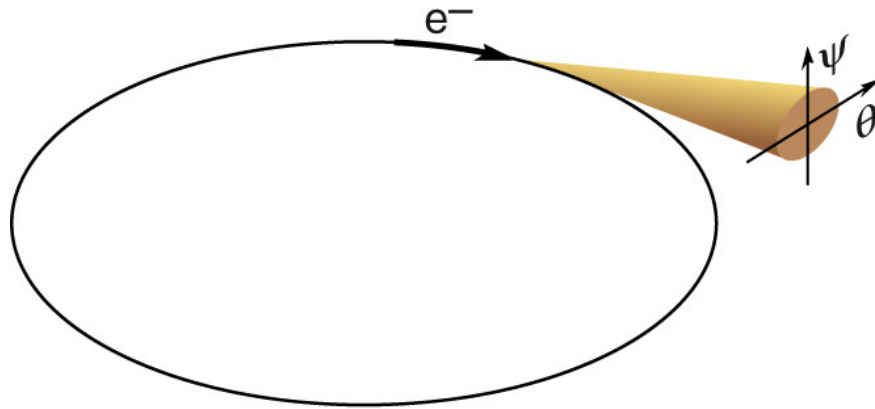
$$\theta \simeq \frac{1}{2\gamma} \quad (5.2)$$



Three forms of synchrotron radiation



Bending magnet radiation covers a broad region of the spectrum, including the primary absorption edges of most elements



$$E_c = \hbar\omega_c = \frac{3e\hbar B\gamma^2}{2m} \quad (5.7a)$$

$$E_c(\text{keV}) = 0.6650 E_e^2(\text{GeV}) B(\text{T}) \quad (5.7b)$$

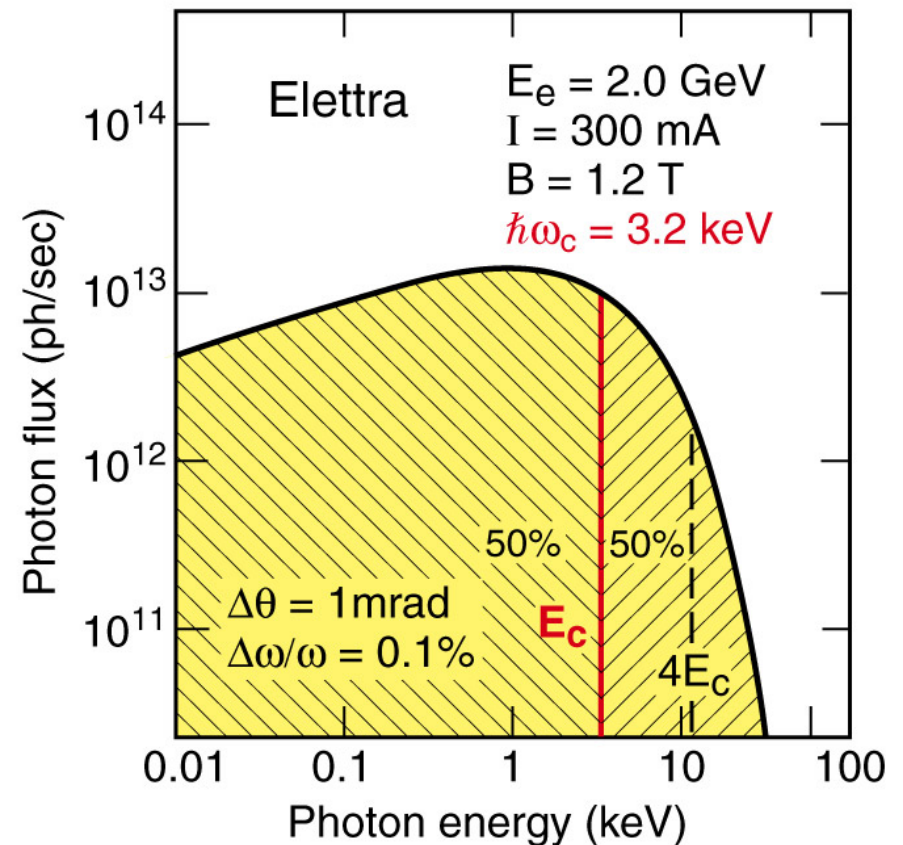
$$\gamma = \frac{E_e}{mc^2} = 1957 E_e(\text{GeV}) \quad (5.5)$$

Advantages:

- covers broad spectral range
- least expensive
- most accessible

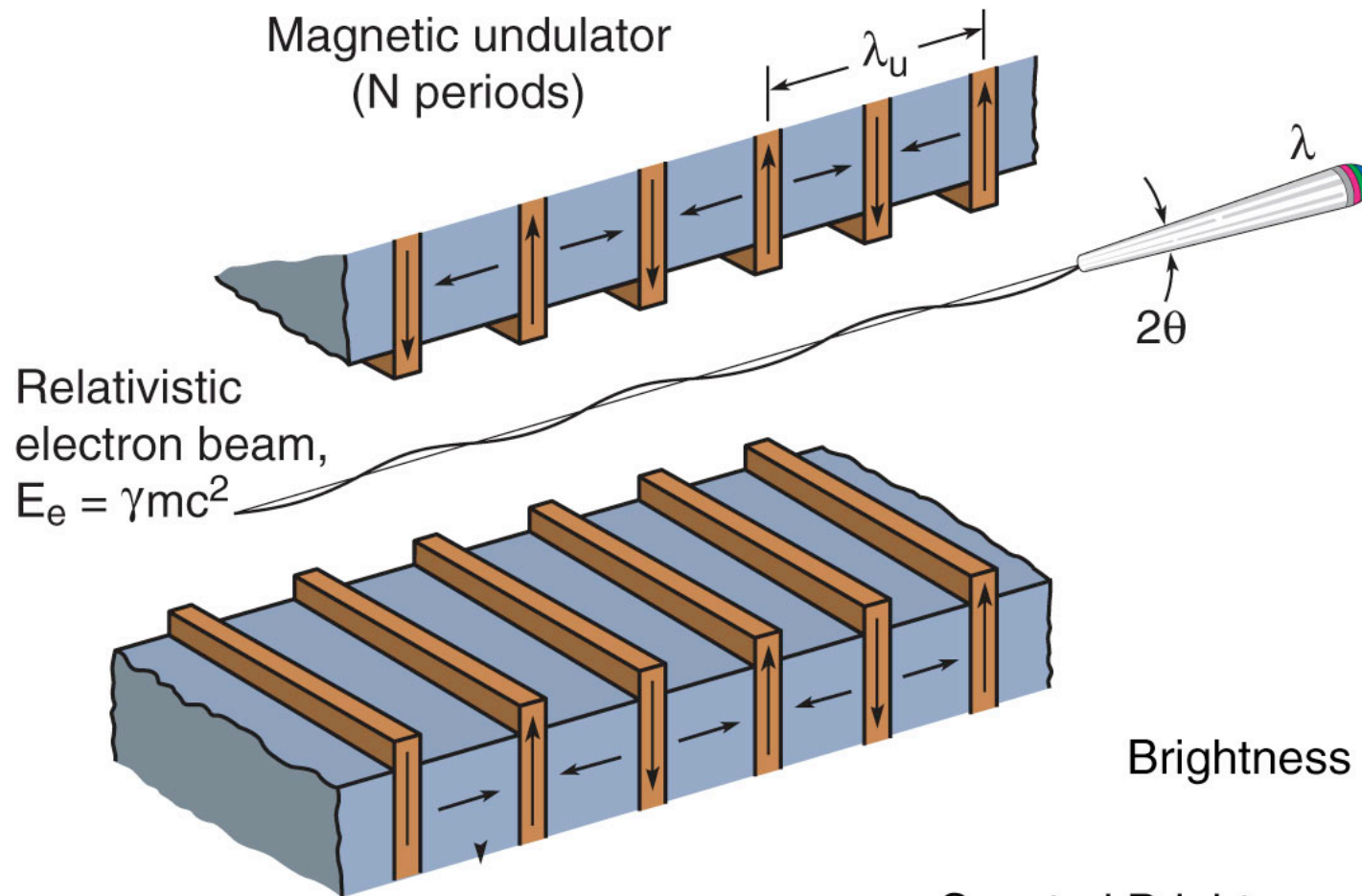
Disadvantages:

- limited coverage of hard x-rays
- not as bright as undulator



What is E_c at a facility near you?
What is $4E_c$?

Undulator radiation from a small electron beam radiating into a narrow forward cone is very bright



$$\lambda \approx \frac{\lambda_u}{2\gamma^2}$$

$$\theta_{\text{cen}} \approx \frac{1}{\gamma\sqrt{N}}$$

$$\left[\frac{\Delta\lambda}{\lambda} \right]_{\text{cen}} = \frac{1}{N}$$

$$\text{Brightness} = \frac{\text{photon flux}}{(\Delta A) (\Delta\Omega)}$$

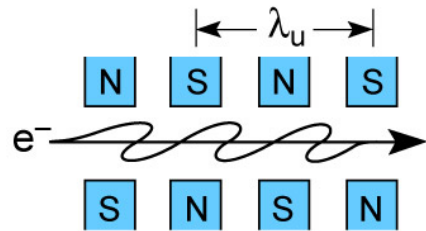
$$\text{Spectral Brightness} = \frac{\text{photon flux}}{(\Delta A) (\Delta\Omega) (\Delta\lambda/\lambda)}$$

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Undulator radiation

Laboratory Frame of Reference

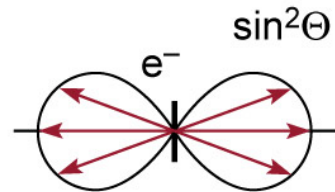


$$E = \gamma mc^2$$

$$\gamma = \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}}$$

$N = \# \text{ periods}$

Frame of Moving e^-



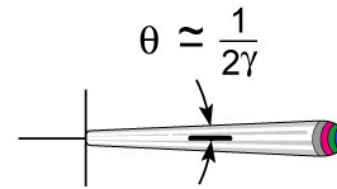
e^- radiates at the Lorentz contracted wavelength:

$$\lambda' = \frac{\lambda_u}{\gamma}$$

Bandwidth:

$$\frac{\lambda'}{\Delta \lambda'} \simeq N$$

Frame of Observer



Doppler shortened wavelength on axis:

$$\lambda = \lambda' \gamma (1 - \beta \cos \theta)$$

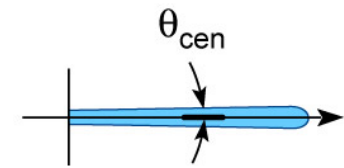
$$\lambda = \frac{\lambda_u}{2\gamma^2} (1 + \gamma^2 \theta^2)$$

Accounting for transverse motion due to the periodic magnetic field:

$$\lambda = \frac{\lambda_u}{2\gamma^2} \left(1 + \frac{K^2}{2} + \gamma^2 \theta^2 \right)$$

where $K = eB_0 \lambda_u / 2\pi mc$

Following Monochromator



$$\text{For } \frac{\Delta \lambda}{\lambda} \simeq \frac{1}{N}$$

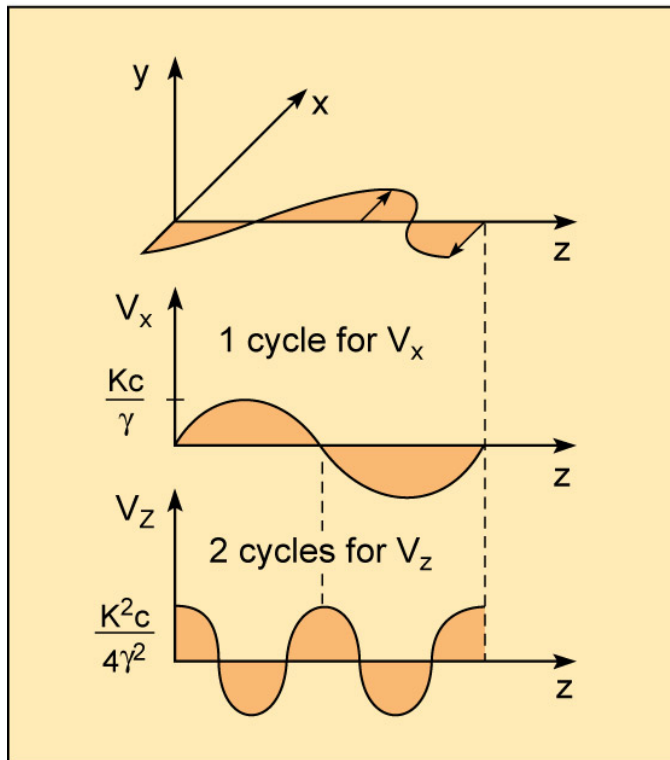
$$\theta_{\text{cen}} \simeq \frac{1}{\gamma \sqrt{N}}$$

typically

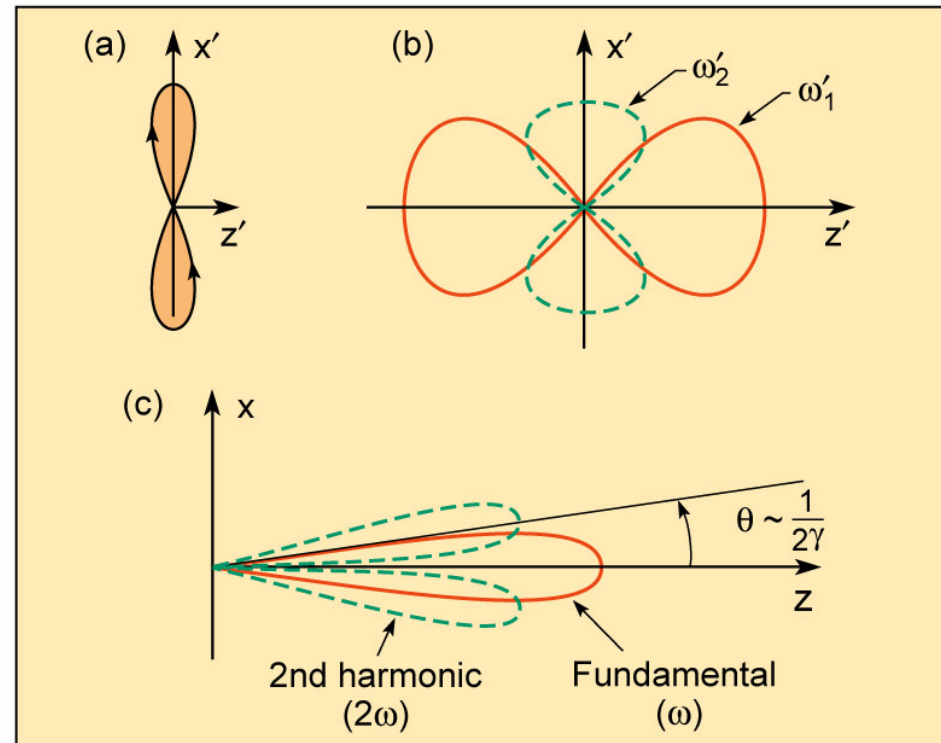
$$\theta_{\text{cen}} \simeq 40 \mu\text{rad}$$

Comments on undulator harmonics

First and second harmonic motions



Radiation patterns in the electron and laboratory frames



$$\lambda_n = \frac{\lambda_u}{2\gamma^2 n} \left(1 + \frac{K^2}{2} + \gamma^2 \theta^2 \right) \quad (5.30)$$

$$\left(\frac{\Delta\lambda}{\lambda} \right)_n = \frac{1}{nN} \quad (5.31)$$



Undulator harmonics

Recall that the axial velocity has a double frequency component

$$v_z = c \left[1 - \frac{1 + K^2/2}{2\gamma^2} + \frac{K^2}{4\gamma^2} \cos(2k_u z) \right]$$

which in the frame of reference moving with the electrons, gives

$$z'(t') \simeq \frac{K^2}{8k'_u} \sin 2\omega'_u t' \quad (5.70)$$

where $k'_u = \gamma^* k_u$ and $\omega'_u = \gamma^* \omega_u$. The transverse motion in this frame is

$$x'(t') \simeq -\frac{K}{k_u \gamma} \cos \omega_u \gamma^* \left(t' + \frac{z'}{c} \right)$$

To a higher degree of accuracy, we now keep the z'/c term

$$x'(t') \simeq -\frac{K}{k'_u} \cos \left(\omega'_u t' + \frac{K^2}{8} \sin 2\omega'_u t' \right) \quad (5.71)$$

for small K

$$x'(t') \simeq -\frac{1}{k'_u} \left[K \cos \omega'_u t' + \frac{K^3}{16} \cos 3\omega'_u t' \right] \quad (5.72)$$

Taking second derivatives to find acceleration, and squaring $|a'(t')|^2$

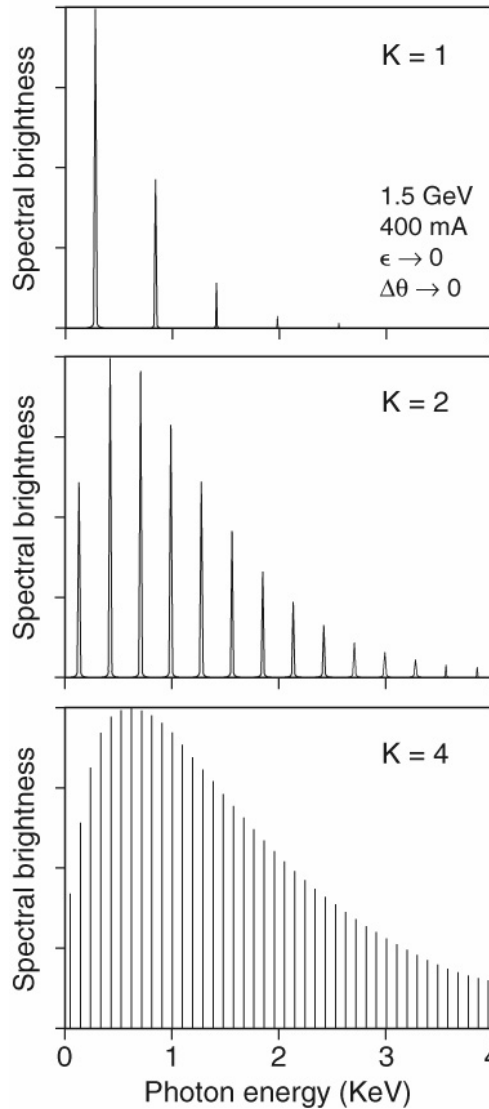
$$\frac{dP'}{d\Omega'} \propto n^4 K^{2n}$$

Thus harmonics grow very rapidly for $K > 1$.

The transition from undulator radiation ($K \leq 1$) to wiggler radiation ($K \gg 1$)



$\lambda_u = 5 \text{ cm}, N = 89$



Undulator radiation ($K \leq 1$)

- Narrow spectral lines
- High spectral brightness
- Partial coherence

$$\lambda = \frac{\lambda_u}{2\gamma^2} \left(1 + \frac{K^2}{2} + \gamma^2 \theta^2 \right)$$

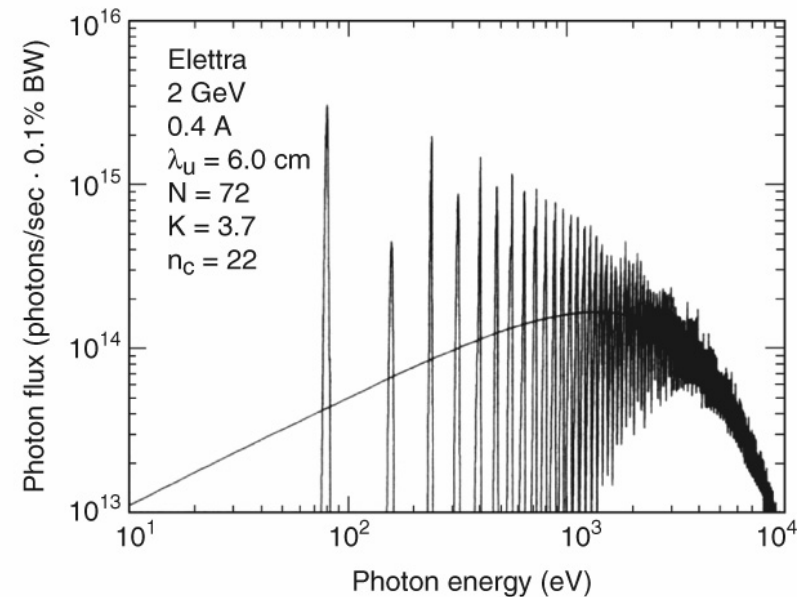
$$K = \frac{eB_0\lambda_u}{2\pi mc}$$

Wiggler radiation ($K \gg 1$)

- Higher photon energies
- Spectral continuum
- Higher photon flux ($2N$)

$$\hbar\omega_c = \frac{3}{2} \frac{\hbar\gamma^2 eB_0}{m}$$

$$n_c = \frac{3K}{4} \left(1 + \frac{K^2}{2} \right)$$

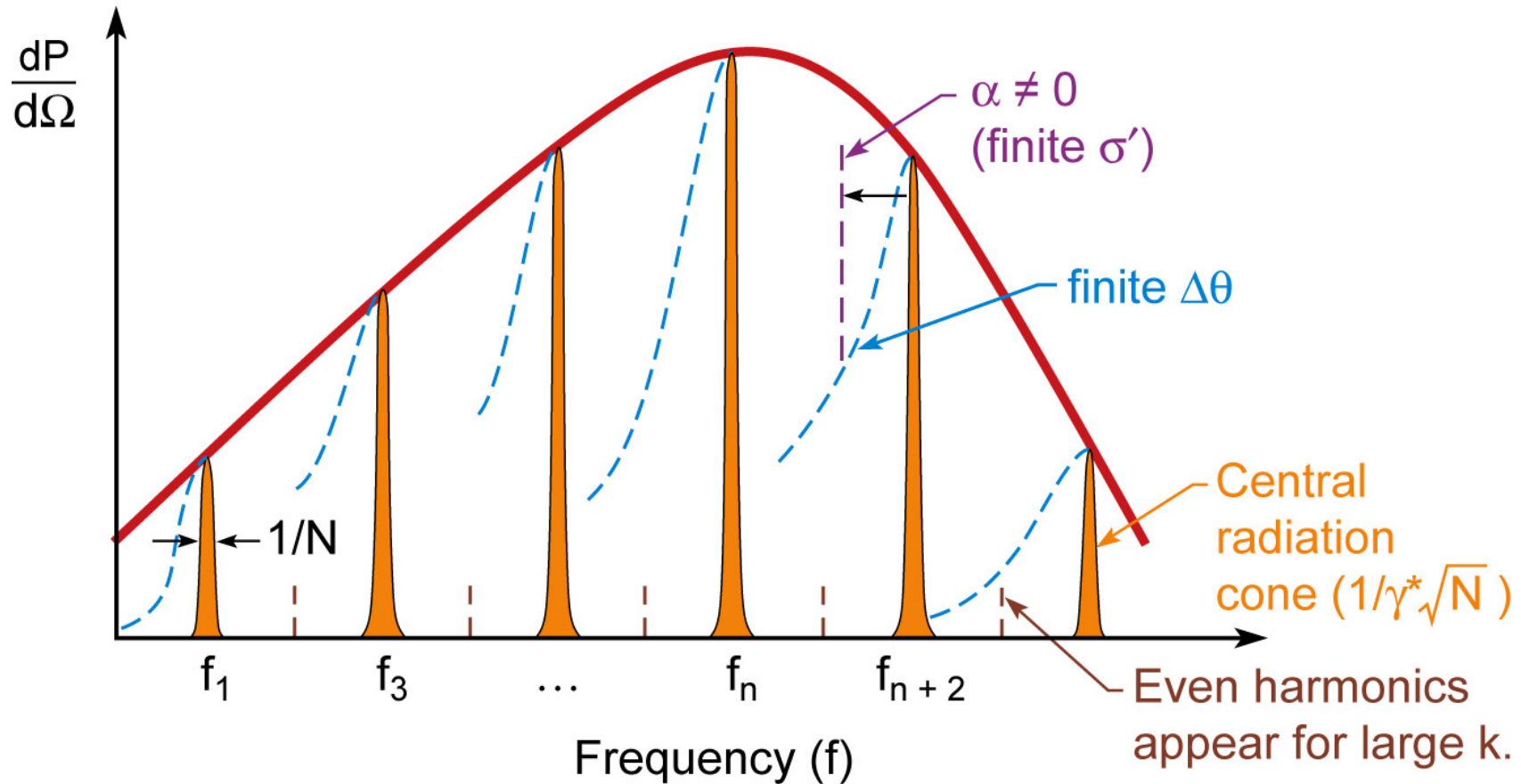


Courtesy of R.P. Walker (Diamond, UK)
and B. Diviacco (Elettra, Trieste, Italy)

Courtesy of K.-J. Kim



For very large $K \gg 1$, and large $\Delta\theta$, a continuum emerges



Ch05_F31VG.ai

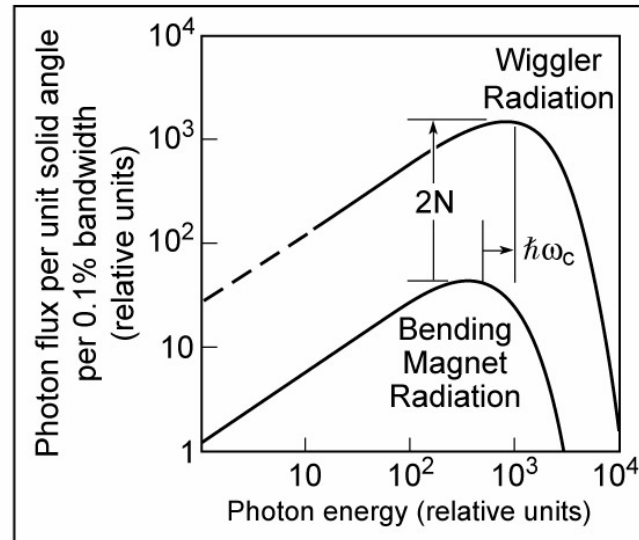
Wiggler radiation

At very high $K \gg 1$, the radiated energy appears in very high harmonics, and at rather large horizontal angles $\theta \approx \pm K/\gamma$ (eq. 5.21). Because the emission angles are large, one tends to use larger collection angles, which tends to spectrally merge nearby harmonics. The result is a continuum at very high photon energies, similar to that of bending magnet radiation, but increased by $2N$ (the number of magnet pole pieces).

$$E_c = \hbar\omega_c = \frac{3e\hbar B\gamma^2}{2m} \quad ; \quad n_c = \frac{3K}{4} \left(1 + \frac{K^2}{2}\right) \quad (5.7a \text{ \& } 82)$$

$$\left. \frac{d^2 F}{d\theta d\psi d\omega/\omega} \right|_0 = 2.65 \times 10^{13} N E_e^2 (\text{GeV}) I (\text{A}) H_2(E/E_c) \frac{\text{photons/s}}{\text{mrad}^2 (0.1\% \text{BW})} \quad (5.86)$$

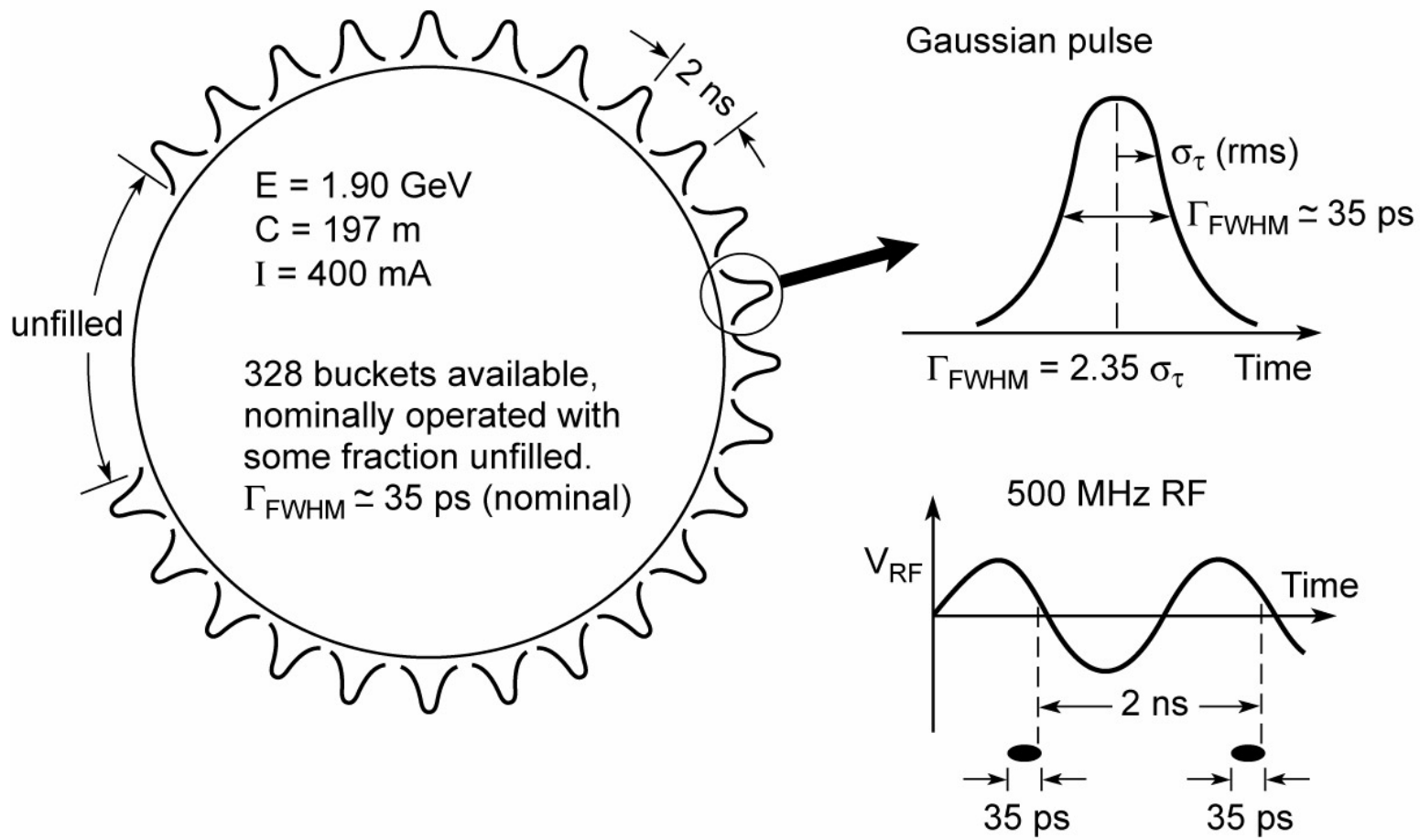
$$\frac{d^2 F}{d\theta d\omega/\omega} = 4.92 \times 10^{13} N E_e (\text{GeV}) I (\text{A}) G_1(E/E_c) \frac{\text{photons/s}}{\text{mrad} \cdot (0.1\% \text{BW})} \quad (5.87)$$



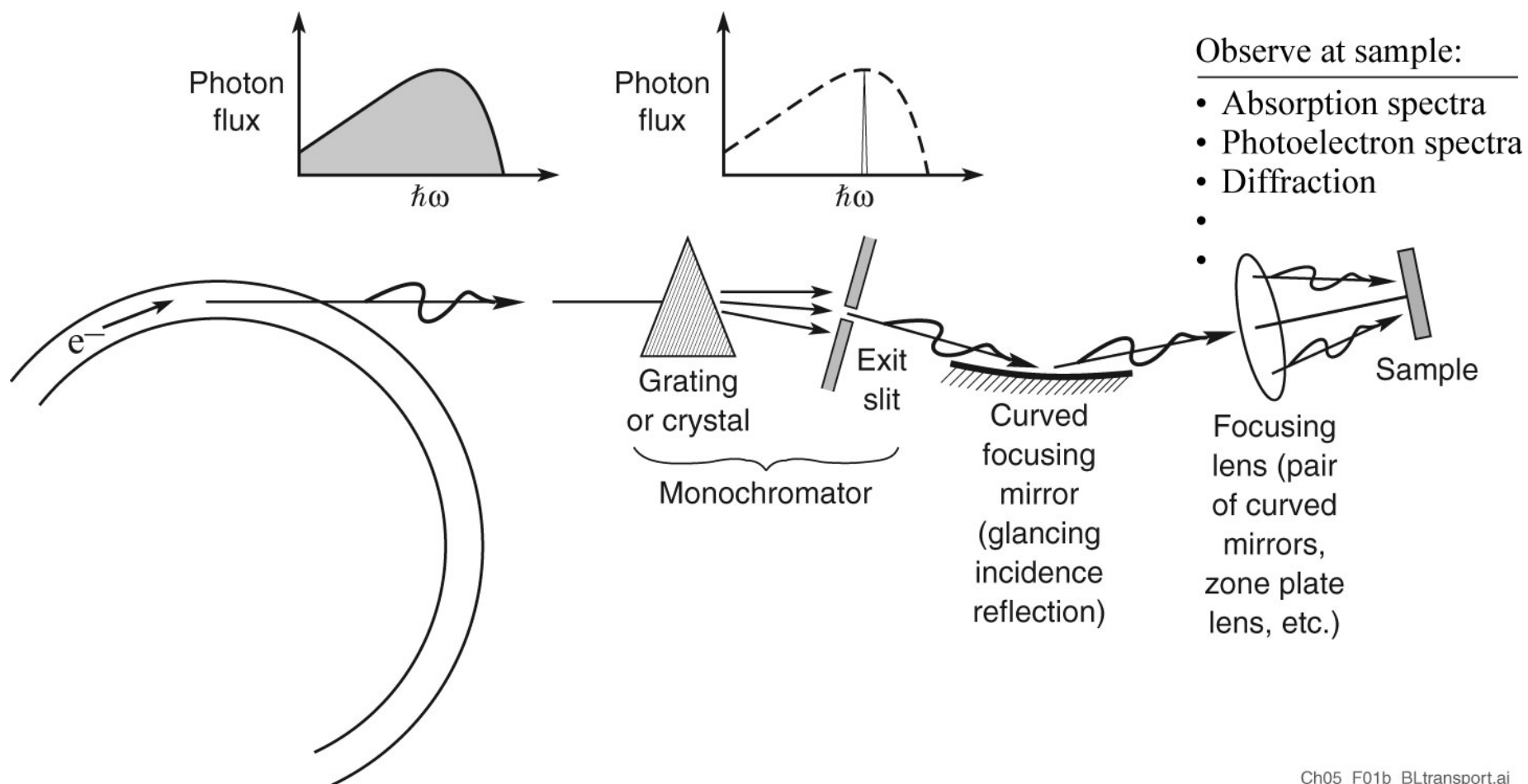
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Time structure of synchrotron radiation

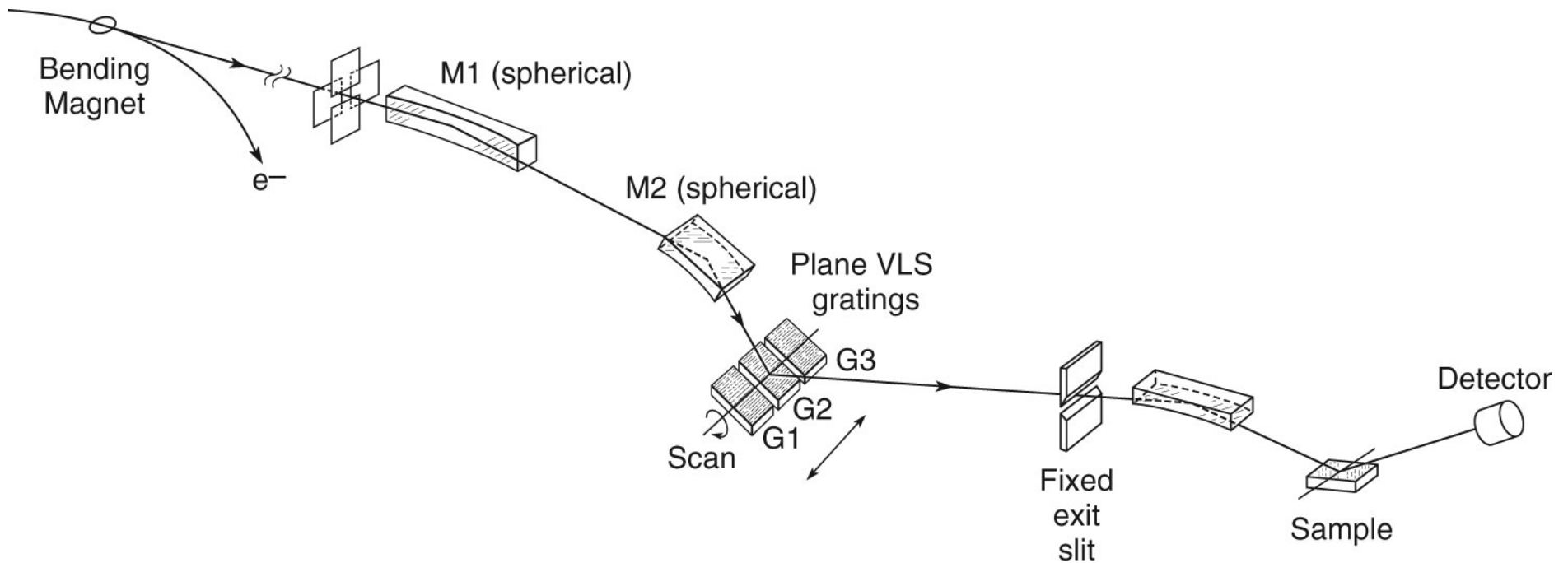
The axial electric field within the RF cavity, used to replenish lost (radiated) energy, forms a potential well “bucket” system that forces electrons into axial electron “bunches”. This leads to a time structure in the emitted radiation.



Beamlines are used to transport photons to the sample, and take a desired spectral slice



A typical beamline: monochromator plus focusing optics to deliver radiation to the sample

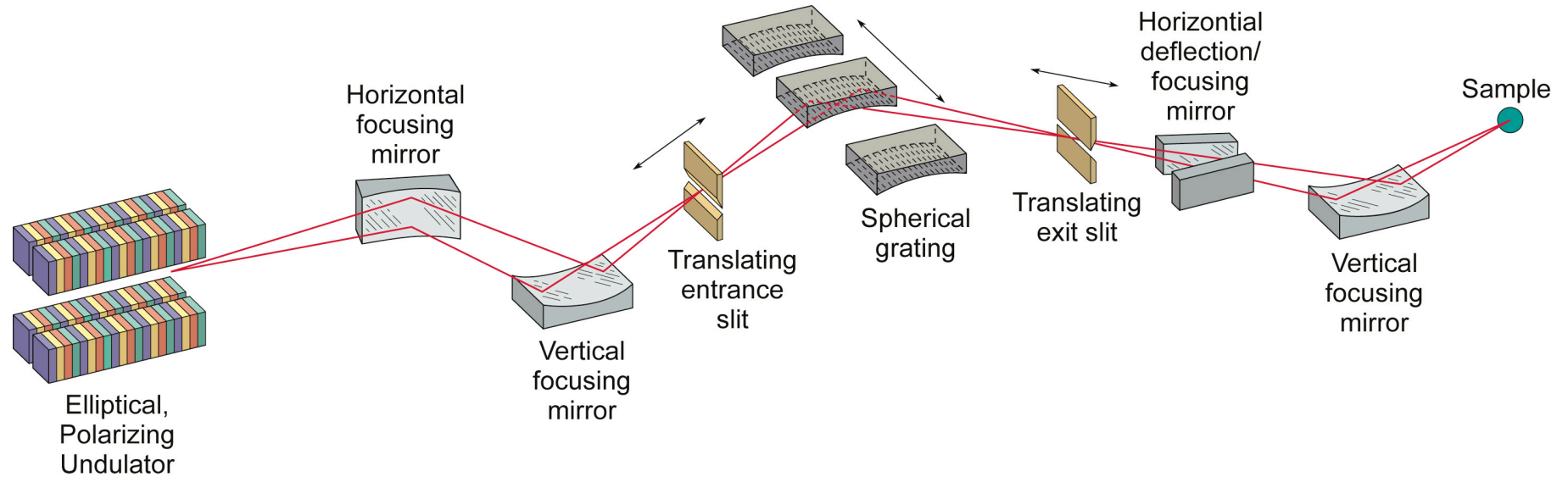


Courtesy of James Underwood (EUV Technology Inc.)

XBD9509-04496rev.1.04.ai



High spectral resolution (meV) beamline



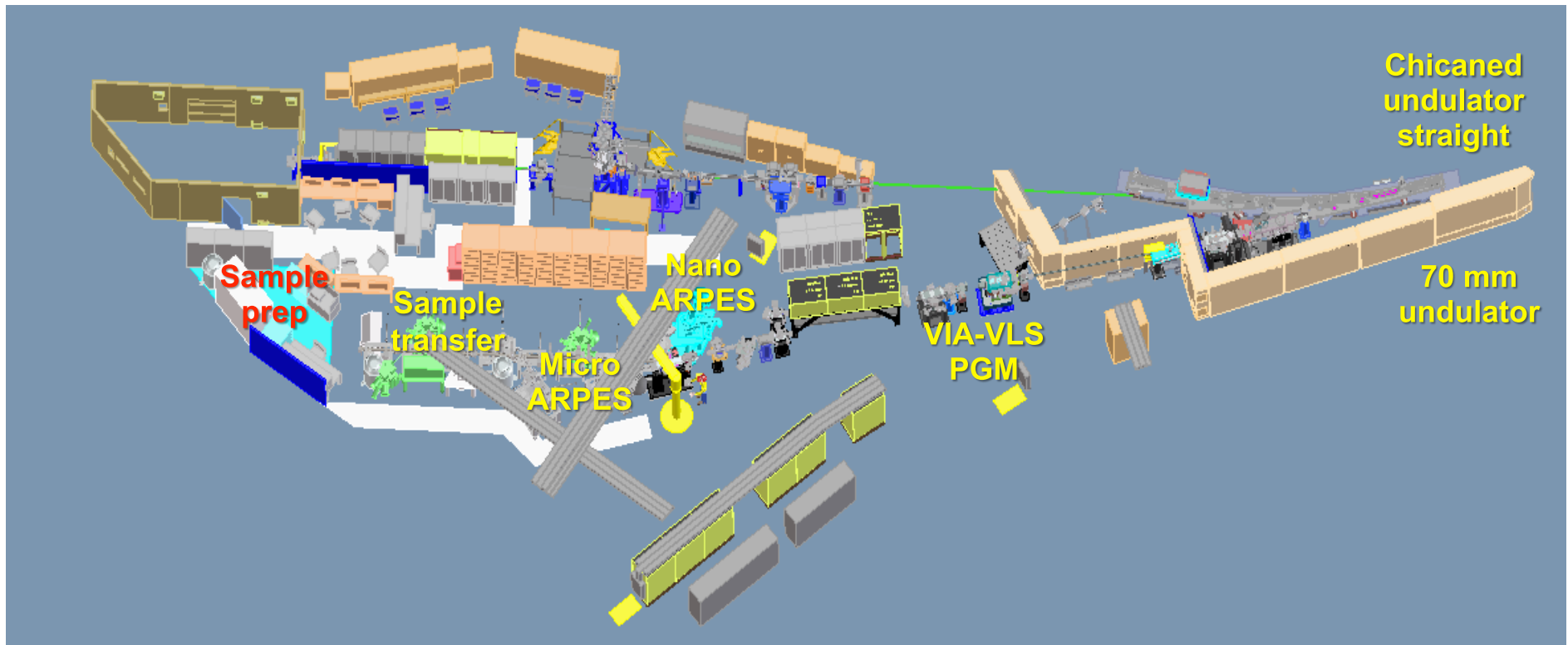
Beamline 7.0 at Berkeley's Advanced Light Source



MAESTRO: A new varied-line-space grating monochromator beam line for angle-resolved-photo-electron-spectroscopy with high spectral and spatial resolution at the Advanced Light Source



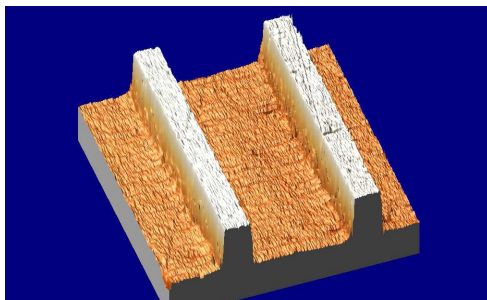
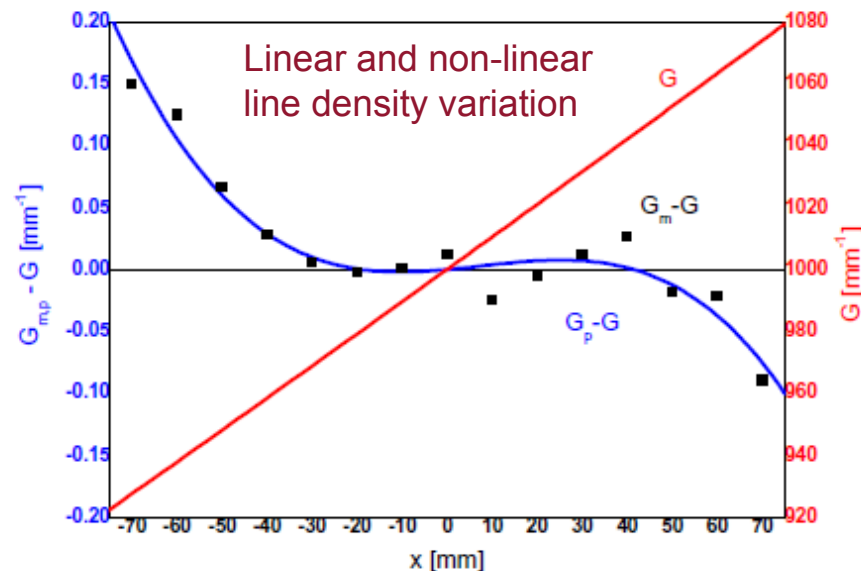
Jason Wells, Derek Yegian, Ken Chow, Eli Rotenberg, Aaron Bostwick, Geoff Gaines and Tony Warwick



The latest soft x-ray undulator spectroscopy beam line planned for the ALS serves **MAESTRO** a new high resolution Angle Resolved Photo Emission facility with zone-plate focused nano-ARPES. The beam line design offers spectral resolution 1:30000 from 60eV to 400eV with an extended energy range from 20eV to 1000eV. Challenges include optical figure quality, thermal engineering, source size and stability and vibrations in the monochromator. The optical design is radical in that a VLS grating will provide all of the focusing in the dispersion direction, and the mirrors are plane, except for a sphere to collect and focus horizontally.

Varied line space gratings

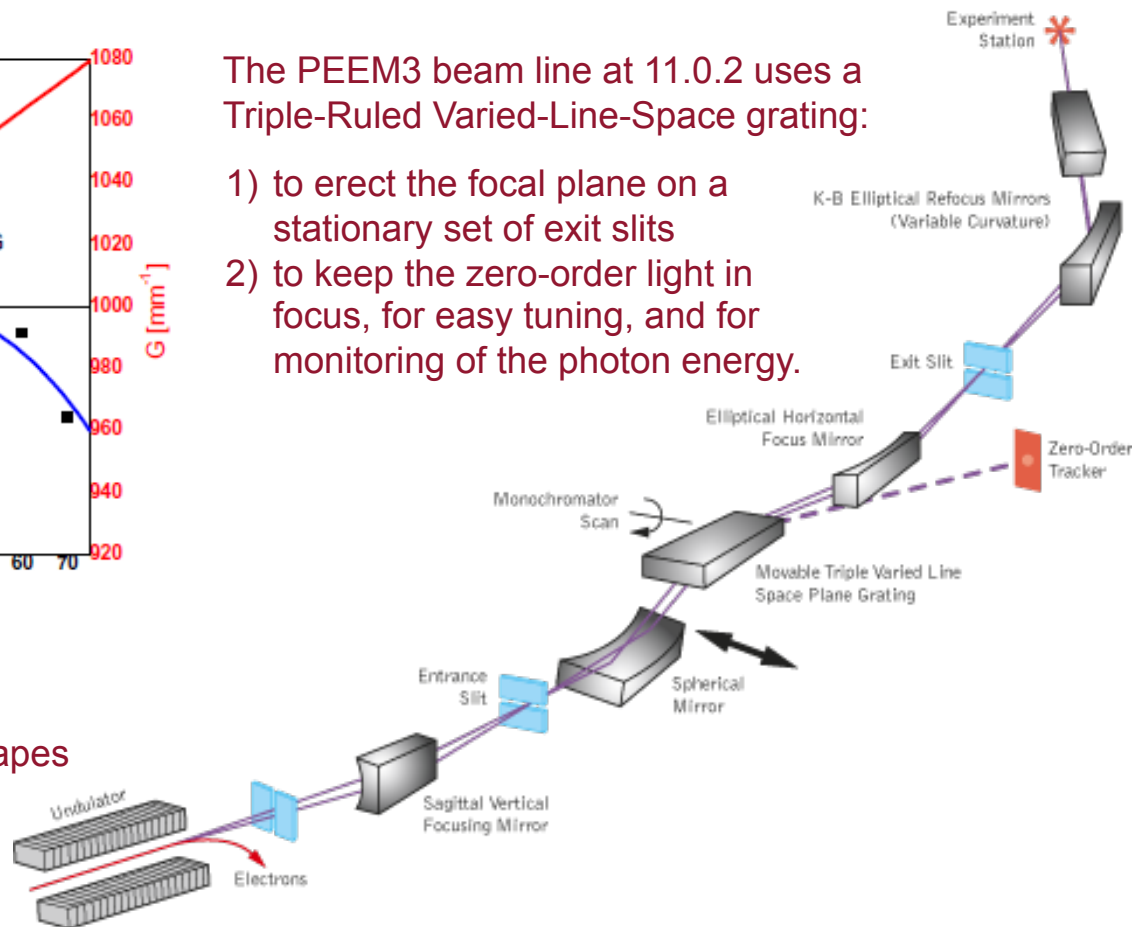
Varied-Line-Space Plane Gratings provide focusing and aberration correction along with the dispersion that they generate in the monochromator. They can be used to erect the monochromator focal plane, making the position of the focus at the exit slit (almost) stationary as the grating rotates to select the photon energy. Beyond that, they are now being used to replace the focusing from shaped optics, making beam lines cheaper and easier to align.



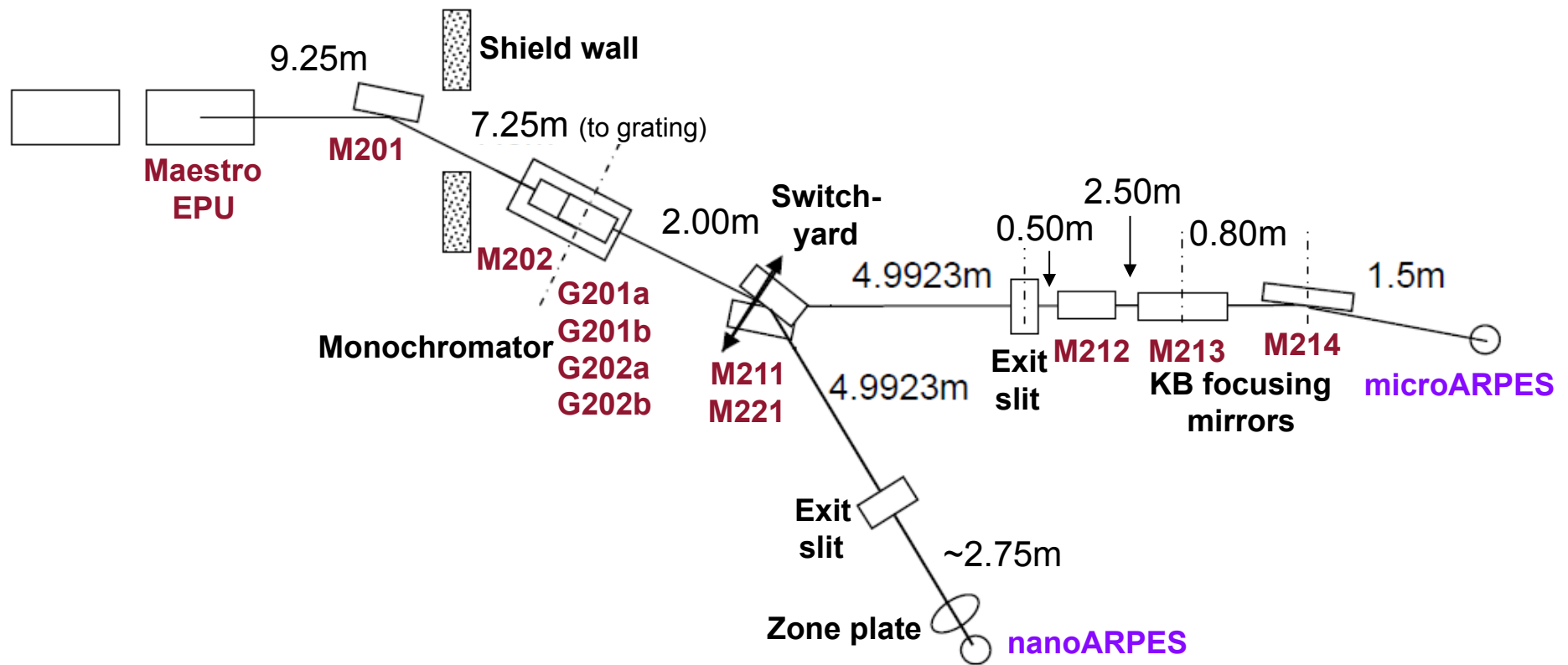
AFM measured groove shapes

The PEEM3 beam line at 11.0.2 uses a Triple-Ruled Varied-Line-Space grating:

- 1) to erect the focal plane on a stationary set of exit slits
- 2) to keep the zero-order light in focus, for easy tuning, and for monitoring of the photon energy.

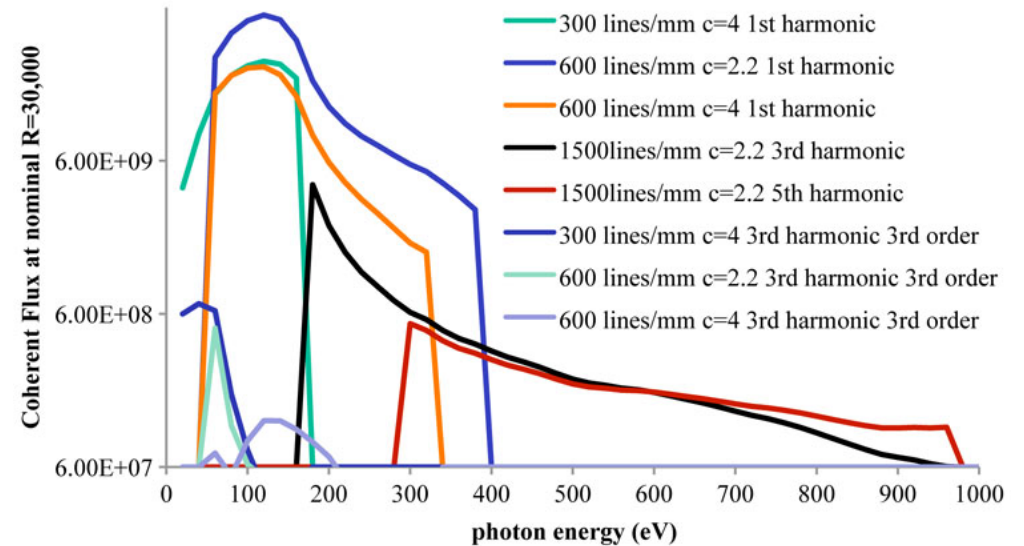
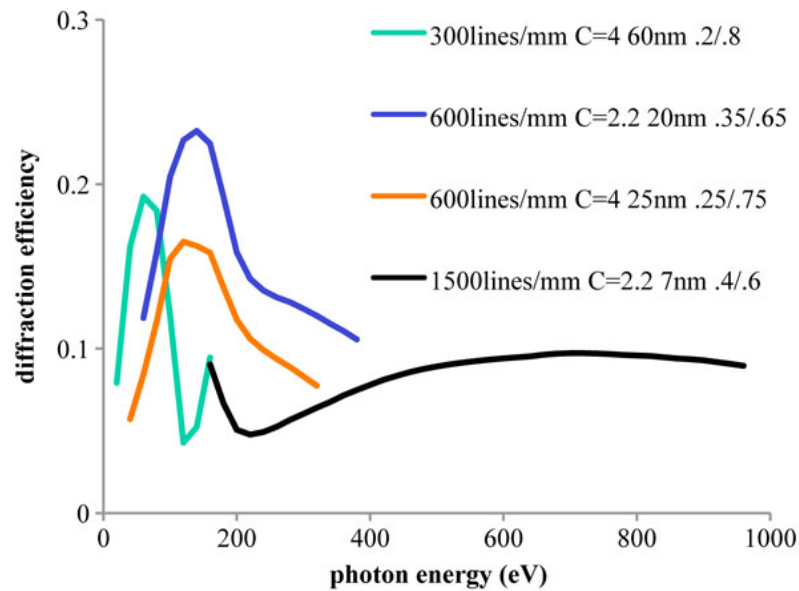


MAESTRO: A new varied-line-space grating monochromator beam line at the ALS

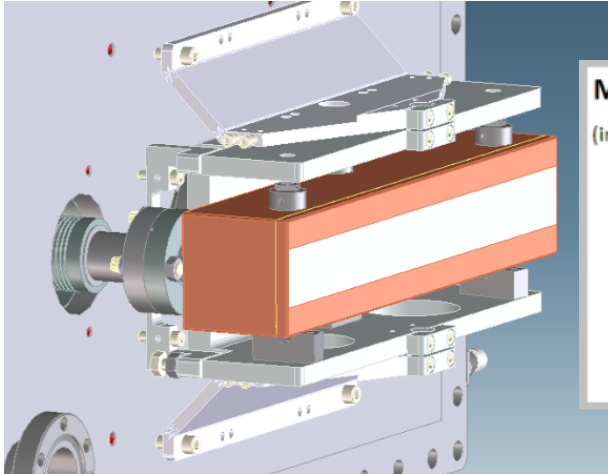




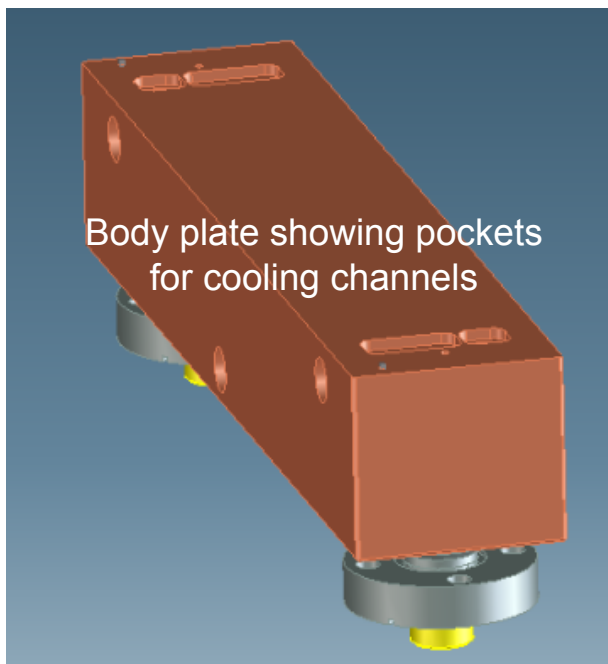
MAESTRO at the ALS: gratings and efficiencies



Water-cooled optics are essential: correcting slope errors due to a thermal bump



M201 Plane - Slope Errors (μRad) (internally cooled Glidcop, $10\text{K W/m}^2\text{K}$)	<u>over full mirror substrate</u>		<u>over clear aperture</u>	
	60eV	20eV	60eV	20eV
Maximum Tangential Slope Error	28.2	61.3	28.2	61.3
Average Tangential Slope Error	2.4	4.9	3.0	6.1
RMS Tangential Slope Error	3.3	7.0	4.4	9.3
Maximum Sagittal Slope Error	36.4	75.1	36.4	75.1
Average Sagittal Slope Error	7.3	15.3	13.9	29.2
RMS Sagittal Slope Error	12.2	25.6	18.0	38.0



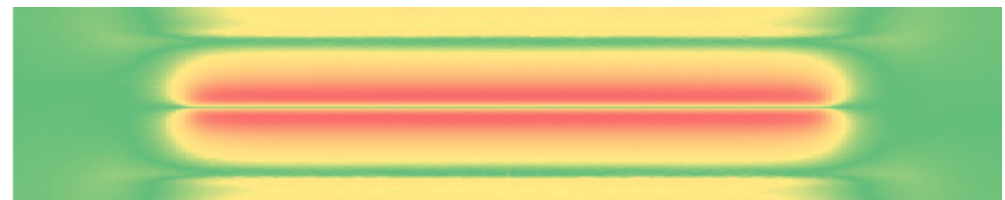
Height error



Tangential slope error



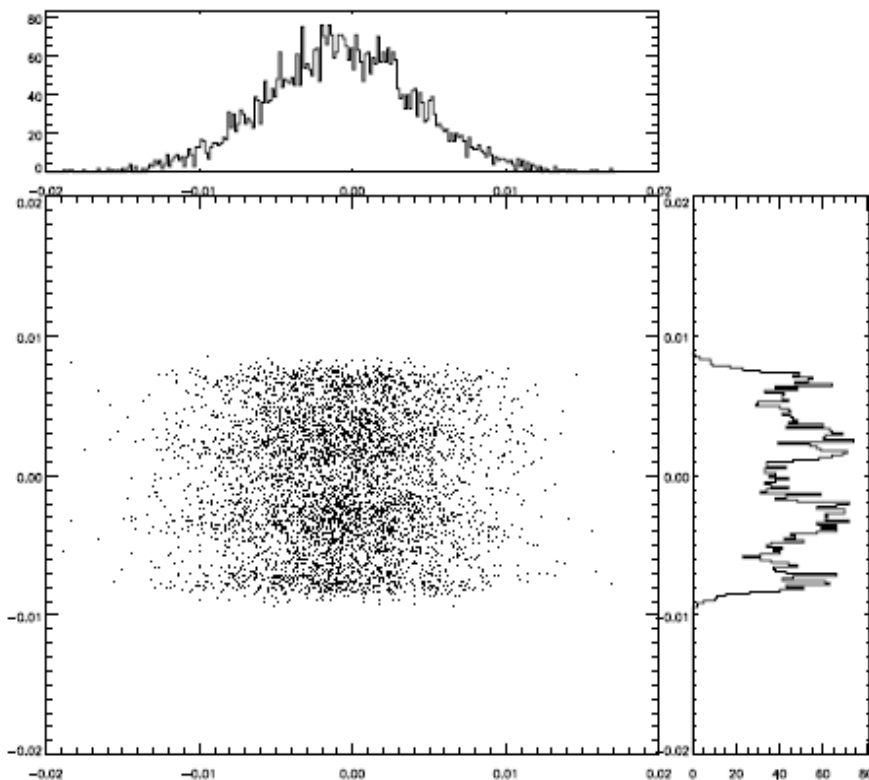
Sagittal slope error



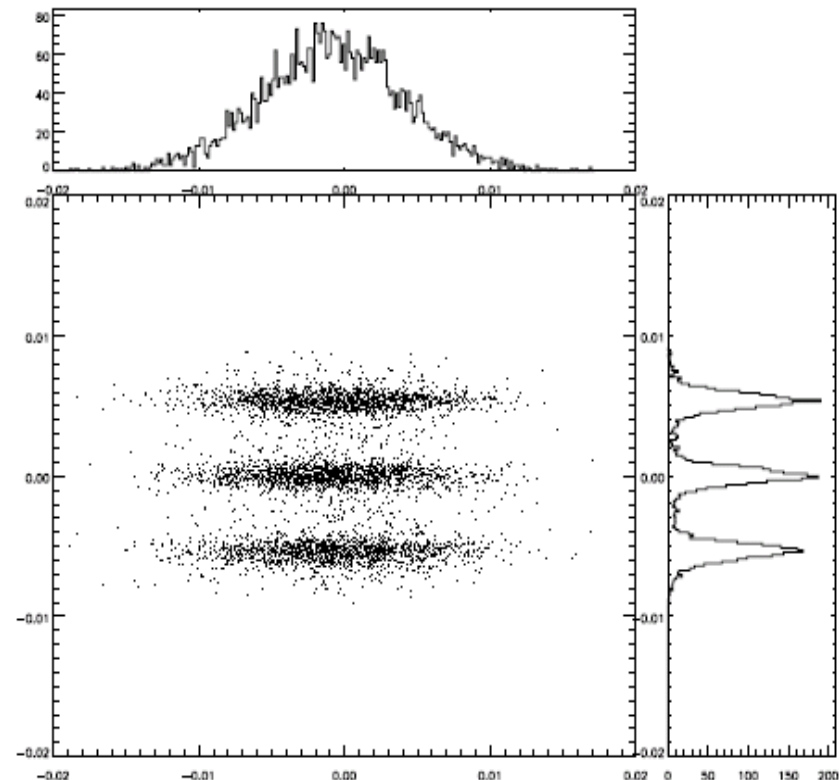


Ray tracing beamlines is an important tool

Significant degradation of the spectral resolution occurs due to localized heating of M202. It is almost entirely corrected by adjusting the monochromator focusing parameter from 3.93 to 4.02. The engineering design will allow this mirror to be built with 1mm thick hot-wall and the actual thermal deformation is expected to be less.



600lines_60eV_10000_c=3.93034_18.7_0.038_
1.5mmheatbump



600lines_60eV_10000_c=4.02_18.7_0.038_
1.5mmheatbumpcorrected



References

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Peterson, H., Jung, C., Hellwig, C. Peatman, W.B. and Gudat, W., Rev. Sci. Instrum. 66 (1995) 1

Follath, R., and Senf, F., Nucl. Instrum. Methods Phys. Res. A390 (1997) 388

Amemiya, K., Kitajima, Y., Ohta, T., and Ito, K., J. Synchrotron Radiation 3 (1996) 282

The original SHADOW package is available at www.nanotech.wisc.edu/CNTLABS/shadow.html and with an IDL user interface at www.esrf.fr/computing/scientific/xop

Undulator Radiation, Ellaume, P., in Undulators, Wigglers and their Applications, Onuki, H. and Ellaume, P. eds., Taylor and Francis.

Characteristics of Synchrotron Radiation, Kim, K., J., in Xray Data Booklet LBNL internal report (1986) PUB 490 xdb.lbl.gov/xdb.pdf

D Fluckiger - Grating Solver Development Company Dec 2006 www.gsolver.com



What are the relative merits?

Bending magnet radiation

- Broad spectrum
- Good photon flux
- No heat load
- Less expensive
- Easier access

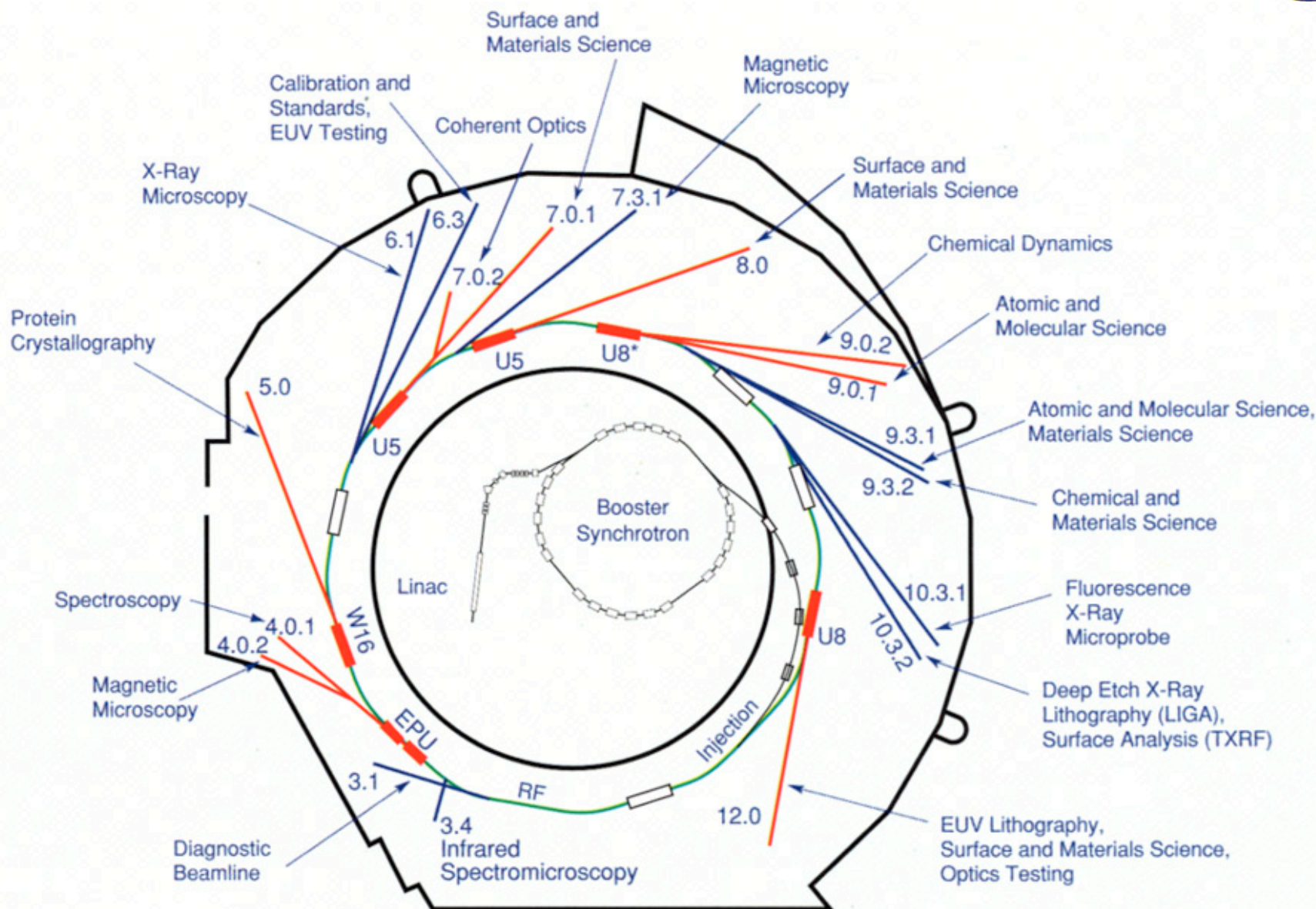
Wiggler radiation

- Higher photon energies
- More photon flux
- Expensive magnet structure
- Expensive cooled optics
- Less access

Undulator radiation

- Brighter radiation
- Smaller spot size
- Partial coherence
- Expensive
- Less access

A single storage ring serves many scientific user groups





Typical parameters for synchrotron radiation

Facility	ALS	ELETTRA	Australian Synchrotron	APS
Electron energy	1.90 GeV	2.0 GeV	3.0 GeV	7.00 GeV
γ	3720	3910	5871	13,700
Current (mA)	400	300	200	100
Circumference (m)	197	259	216	1100
RF frequency (MHz)	500	500	500	352
Pulse duration (FWHM) (ps)	35-70	37	~100	100
<i>Bending Magnet Radiation:</i>				
Bending magnet field (T)	1.27	1.2	1.31	0.599
Critical photon energy (keV)	3.05	3.2	7.84	19.5
Critical photon wavelength	0.407 nm	0.39 nm	1.58 Å	0.636 Å
Bending magnet sources	24	12	28	35
<i>Undulator Radiation:</i>				
Number of straight sections	12	12	14	40
Undulator period (typical) (cm)	5.00	5.6	22.0	3.30
Number of periods	89	81	80	72
Photon energy ($K = 1, n = 1$)	457 eV	452 eV	2.59 keV	9.40 keV
Photon wavelength ($K = 1, n = 1$)	2.71 nm	2.74 nm	0.478 nm	1.32 Å
Tuning range ($n = 1$)	230-620 eV	2.0-6.7 nm	0.319-0.835 nm	3.5-12 keV
Tuning range ($n = 3$)	690-1800 eV	0.68-2.2 nm	0.106-0.278 nm	10-38 keV
Central cone half-angle ($K = 1$)	35 μ rad	35 μ rad	23 μ rad	11 μ rad
Power in central cone ($K = 1, n = 1$) (W)	2.3	1.7	6.6	12
Flux in central cone (photons/s)	3.1×10^{16}	2.3×10^{16}	1.6×10^{16}	7.9×10^{15}
σ_x, σ_y (μ m)	260, 16	255, 23	320, 16	320, 50
σ'_x, σ'_y (μ rad)	23, 3.9	31, 9	34, 6	23, 7
Brightness ($K = 1, n = 1$) ^a [(photons/s)/mm ² · mrad ² · (0.1%BW)]	2.3×10^{19}	9.9×10^{18}	1.3×10^{19}	5.9×10^{18}
Total power ($K = 1$, all n , all θ) (W)	83	126	476	350
Other undulator periods (cm)	3.65, 8.00, 10.0	8.0, 12.5	6.8, 18.3	2.70, 5.50, 12.8
<i>Wiggler Radiation:</i>				
Wiggler period (typical) (cm)	16.0	14.0	6.1	8.5
Number of periods	19	30	30	28
Magnetic field (maximum) (T)	2.1	1.5	1.9	1.0
K (maximum)	32	19.6	12	7.9
Critical photon energy (keV)	5.1	4.0	11.4 keV	33
Critical photon wavelength	0.24 nm	0.31 nm	0.11 nm	0.38 Å
Total power (max. K) (kW)	13	7.2	9.3	7.4

^aUsing Eq. (5.65). See comments following Eq. (5.64) for the case where $\sigma'_{x,y} \approx \theta_{\text{cen}}$.

Ch05_T1c_AustralSynch_Nov05.ai



Typical parameters for synchrotron radiation

Facility	ALS	MAX II	BESSY II	APS	ESRF
Electron energy	1.90 GeV	1.50 GeV	1.70 GeV	7.00 GeV	6.04 GeV
γ	3720	2940	3330	13,700	11,800
Current (mA)	400	250	200	100	200
Circumference (m)	197	90	240	1100	884
RF frequency (MHz)	500	500	500	352	352
Pulse duration (FWHM) (ps)	35-70	200	20-50	100	70
<i>Bending Magnet Radiation:</i>					
Bending magnet field (T)	1.27	1.48	1.30	0.599	0.806
Critical photon energy (keV)	3.05	2.21	2.50	19.5	19.6
Critical photon wavelength	0.407 nm	0.560 nm	0.50 nm	0.636 Å	0.634 Å
Bending magnet sources	24	20	32	35	32
<i>Undulator Radiation:</i>					
Number of straight sections	12	10	16	40	32
Undulator period (typical) (cm)	5.00	5.20	4.90	3.30	4.20
Number of periods	89	49	84	72	38
Photon energy ($K = 1, n = 1$)	457 eV	274 eV	373 eV	9.40 keV	5.50 keV
Photon wavelength ($K = 1, n = 1$)	2.71 nm	4.53 nm	3.32 nm	1.32 Å	0.225 nm
Tuning range ($n = 1$)	230-620 eV	130-410 eV	140-500 eV	3.5-12 keV	2.6-7.3 keV
Tuning range ($n = 3$)	690-1800 eV	400-1200 eV	410-1100 eV	10-38 keV	7.7-22 keV
Central cone half-angle ($K = 1$)	35 μ rad	59 μ rad	33 μ rad	11 μ rad	17 μ rad
Power in central cone ($K = 1, n = 1$) (W)	2.3	0.88	0.95	12	14
Flux in central cone (photons/s)	3.1×10^{16}	2.0×10^{16}	1.6×10^{16}	7.9×10^{15}	1.6×10^{16}
σ_x, σ_y (μ m)	260, 16	300, 45	314, 24	320, 50	395, 9.9
σ'_x, σ'_y (μ rad)	23, 3.9	26, 20	18, 12	23, 7	11, 3.9
Brightness ($K = 1, n = 1$) ^a [(photons/s)/mm ² · mrad ² · (0.1%BW)]	2.3×10^{19}	7.8×10^{17}	4.6×10^{18}	5.9×10^{18}	5.1×10^{18}
Total power ($K = 1$, all n , all θ) (W)	83	17	32	350	480
Other undulator periods (cm)	3.65, 8.00, 10.0	5.88, 6.60	4.1, 5.6, 12.5	2.70, 5.50, 12.8	2.3, 3.2, 5.2, 8.5
<i>Wiggler Radiation:</i>					
Wiggler period (typical) (cm)	16.0	17.4	12.5	8.5	8.0
Number of periods	19	13	32	28	20
Magnetic field (maximum) (T)	2.1	1.80	1.15	1.0	0.81
K (maximum)	32	29.3	12.8	7.9	6.0
Critical photon energy (keV)	5.1	2.69	2.11	33	20
Critical photon wavelength	0.24 nm	0.46 nm	0.59 nm	0.38 Å	0.62 Å
Total power (max. K) (kW)	13	5.9	1.8	7.4	4.8

^aUsing Eq. (5.65). See comments following Eq. (5.64) for the case where $\sigma'_{x,y} \approx \theta_{\text{cen}}$.

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SOFT X-RAYS AND EXTREME ULTRAVIOLET RADIATION

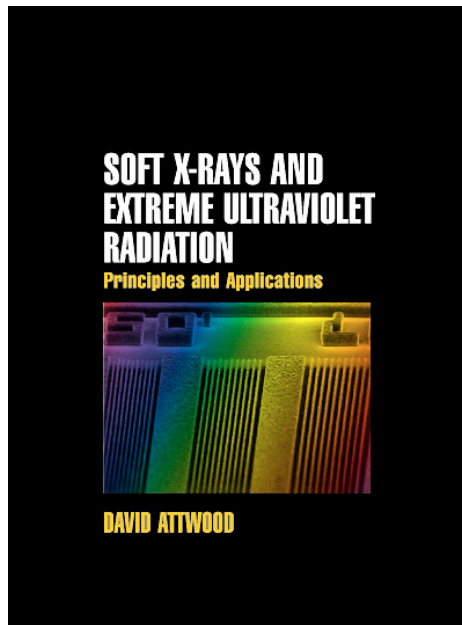
Principles and Applications

DAVID ATTWOOD

UNIVERSITY OF CALIFORNIA, BERKELEY
AND
LAWRENCE BERKELEY
NATIONAL LABORATORY



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